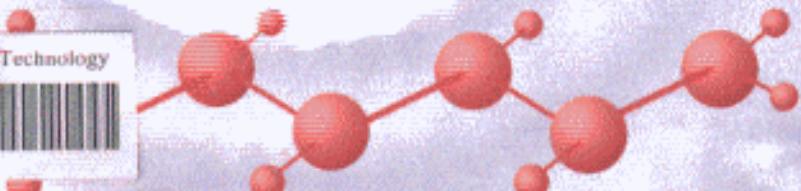


# Principles of Physical Chemistry

Understanding  
Molecules, Molecular Assemblies,  
Supramolecular Machines

$$\Lambda = \frac{h}{mv}$$



Hans Kuhn and Horst-Dieter Försterling

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