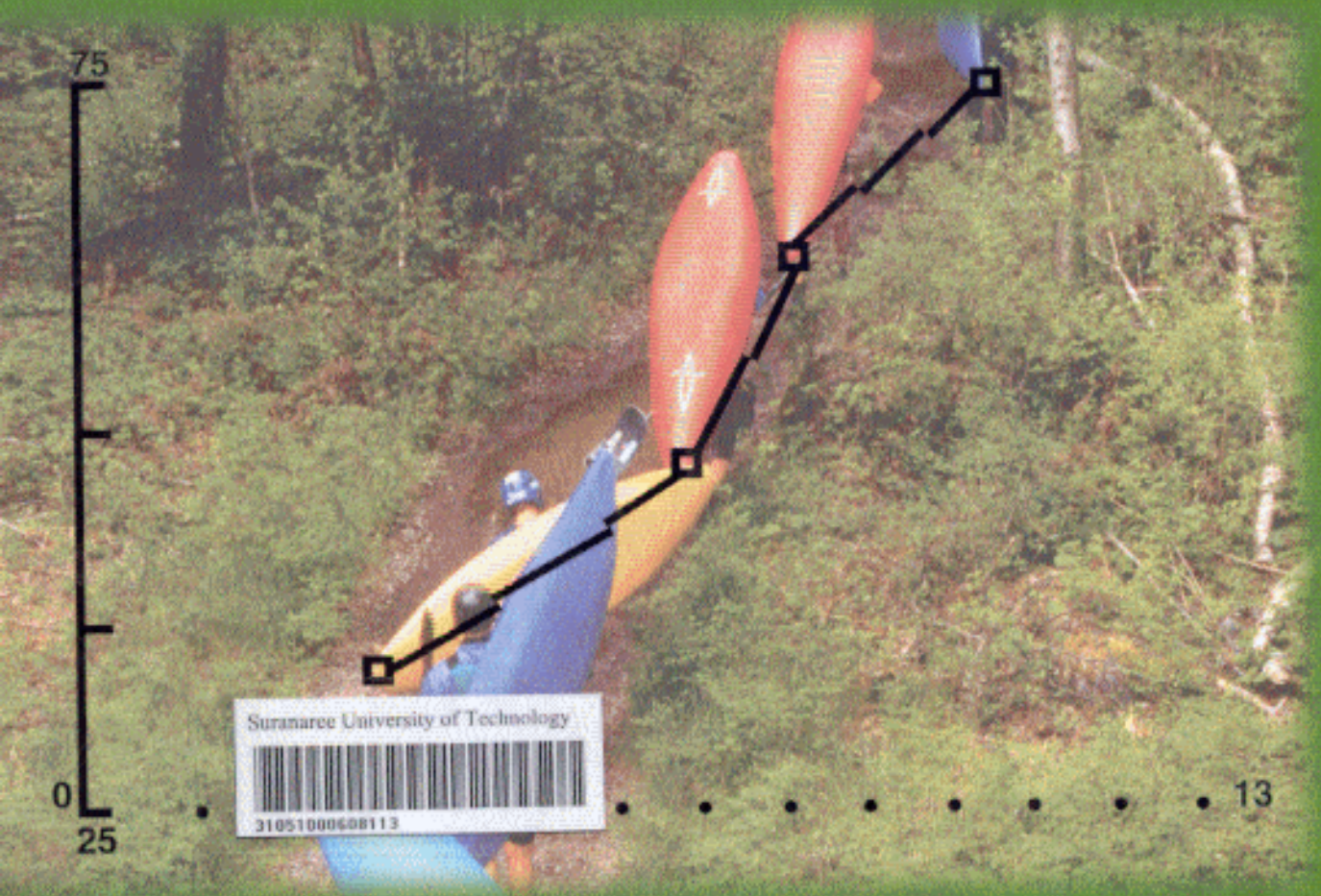
Algebra & Trigonometry

SECOND EDITION

ENHANCED WITH GRAPHING UTILITIES



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CONTENTS

Preface to the Instructor ix
Preface to the Student xiii
List of Application xxiii
Photo Credits xxvii

CHAPTER 1 GRAPHS 1

1.1 Rectangular Coordinates; Graphing Utilities; Scatter Diagrams 2
1.2 Graphs of Equations 15
1.3 Solving Equations 29
1.4 Setting Up Equations; Applications 40
1.5 Solving Inequalities 53
1.6 Lines 66
1.7 Circles 83
Chapter Review 90
Chapter Projects 95

CHAPTER 2 LINEAR AND QUADRATIC FUNCTIONS 97

2.1 Functions 98
2.2 Linear Functions and Models 115
2.3 Quadratic Equations and Functions 124
2.4 Quadratic Functions and Models 139
Chapter Review 150
Chapter Projects 154

CHAPTER 3 FUNCTIONS AND THEIR GRAPHS 155

3.1 Characteristics of Functions; Library of Functions 156
3.2 Graphing Techniques: Transformations 178
3.3 Operations on Functions; Composite Functions 191
3.4 Mathematical Models: Constructing Functions 200
Chapter Review 208
Chapter Projects 212

CHAPTER 4 POLYNOMIAL AND RATIONAL FUNCTIONS 213

4.1 Power Functions and Models 214
4.2 Polynomial Functions and Models 221
4.3 Polynomial Division 234
4.4 The Real Zeros of a Polynomial Function 240
4.5 Complex Numbers; Quadratic Equations with a Negative Discriminant 254
4.6 Complex Zeros; Fundamental Theorem of Algebra 263
4.7 Rational Functions 270
4.8 Polynomial and Rational Inequalities 293
Chapter Review 302
Chapter Projects 307

CHAPTER 5 EXPONENTIAL AND LOGARITHMIC FUNCTIONS 309

5.1 One-to-One Functions; Inverse Functions 310
5.2 Exponential Functions 323
5.3 Logarithmic Functions 337
5.4 Properties of Logarithms 347
5.5 Logarithmic and Exponential Equations 355
5.6 Compound Interest 362
5.7 Growth and Decay 372
5.8 Exponential, Logarithmic, and Logistic Curve Fitting 382
Chapter Review 393
Chapter Projects 398

CHAPTER 6 SYSTEMS OF EQUATIONS AND INEQUALITIES 401

6.1 Systems of Linear Equations: Two Equations Containing Two Variables 402
6.2 Systems of Linear Equations: Three Equations Containing Three Variables 413
6.3 Systems of Linear Equations: Matrices 419
6.4 Systems of Linear Equations: Determinants 434
6.5 Matrix Algebra 445
6.6 Systems of Linear Inequalities; Linear Programming 464
6.7 Partial Fraction Decomposition 481
Chapter Review 488
Chapter Projects 493

CHAPTER 7 TRIGONOMETRIC FUNCTIONS 495

7.1 Angles and Their Measure 496
7.2 Right Triangle Trigonometry 508
7.3 Computing the Values of Trigonometric Functions of Given Angles 519
7.4 Trigonometric Functions of General Angles 526
7.5 Properties of the Trigonometric Functions; Unit Circle Approach 537
7.6 Graphs of the Trigonometric Functions 548
7.7 Sinusoidal Graphs; Sinusoidal Curve Fitting 560
Chapter Review 579
Chapter Projects 585

CHAPTER 8 ANALYTIC TRIGONOMETRY 587

8.1 Trigonometric Identities 589
8.2 Sum and Difference Formulas 594
8.3 Double-Angle and Half-Angle Formulas 603
8.4 Product-to-Sum and Sum-to-Product Formulas 613
8.5 The Inverse Trigonometric Functions 616
8.6 Trigonometric Equations (I) 632
8.7 Trigonometric Equations (II) 637
Chapter Review 644
Chapter Projects 648

CHAPTER 9 APPLICATIONS OF TRIGONOMETRIC FUNCTIONS 651

9.1 Solving Right Triangles 652
9.2 The Law of Sines 661
9.3 The Law of Cosines 673
9.4 The Area of a Triangle 679
9.5 Simple Harmonic Motion; Damped Motion 685
Chapter Review 692
Chapter Projects 697

CHAPTER 10 POLAR COORDINATES; VECTORS 699

10.1 Polar Coordinates 700
10.2 Polar Equations and Graphs 708
10.3 The Complex Plane; DeMoivre's Theorem 728
10.4 Vectors 736
10.5 The Dot Product 747
Chapter Review 757
Chapter Projects 761

CHAPTER 11 ANALYTIC GEOMETRY 763

11.1 Conics 764
11.2 The Parabola 765
11.3 The Ellipse 777
11.4 The Hyperbola 790
11.5 Rotation of Axes; General Form of a Conic 804
11.6 Polar Equations of Conics 813
11.7 Plane Curves and Parametric Equations 819
11.8 Systems of Nonlinear Equations 834
Chapter Review 845
Chapter Projects 849

CHAPTER 12 SEQUENCES; INDUCTION; THE BINOMIAL THEOREM 851

12.1 Sequences 852
12.2 Arithmetic Sequences 864
12.3 Geometric Sequences; Geometric Series 871
12.4 Mathematical Induction 887
12.5 The Binomial Theorem 891
Chapter Review 898
Chapter Projects 902

CHAPTER 13 COUNTING AND PROBABILITY 905

13.1 Sets and Counting 906
13.2 Permutations and Combinations 912
13.3 Probability of Equally Likely Outcomes 922
13.4 Analyzing Univariate Data; Obtaining Probabilities from Data 938
Chapter Review 952
Chapter Projects 957

APPENDIX REVIEW 959

1. Real Numbers 959
2. Algebra Review 973
3. Geometry Review 984
4. Integer Exponents 990
5. Polynomials 998
6. Factoring Polynomials 1006
7. Rational Expressions 1015
8. Square Roots; Radicals 1027
9. Rational Exponents 1035

ANSWERS AN 1
INDEX I1