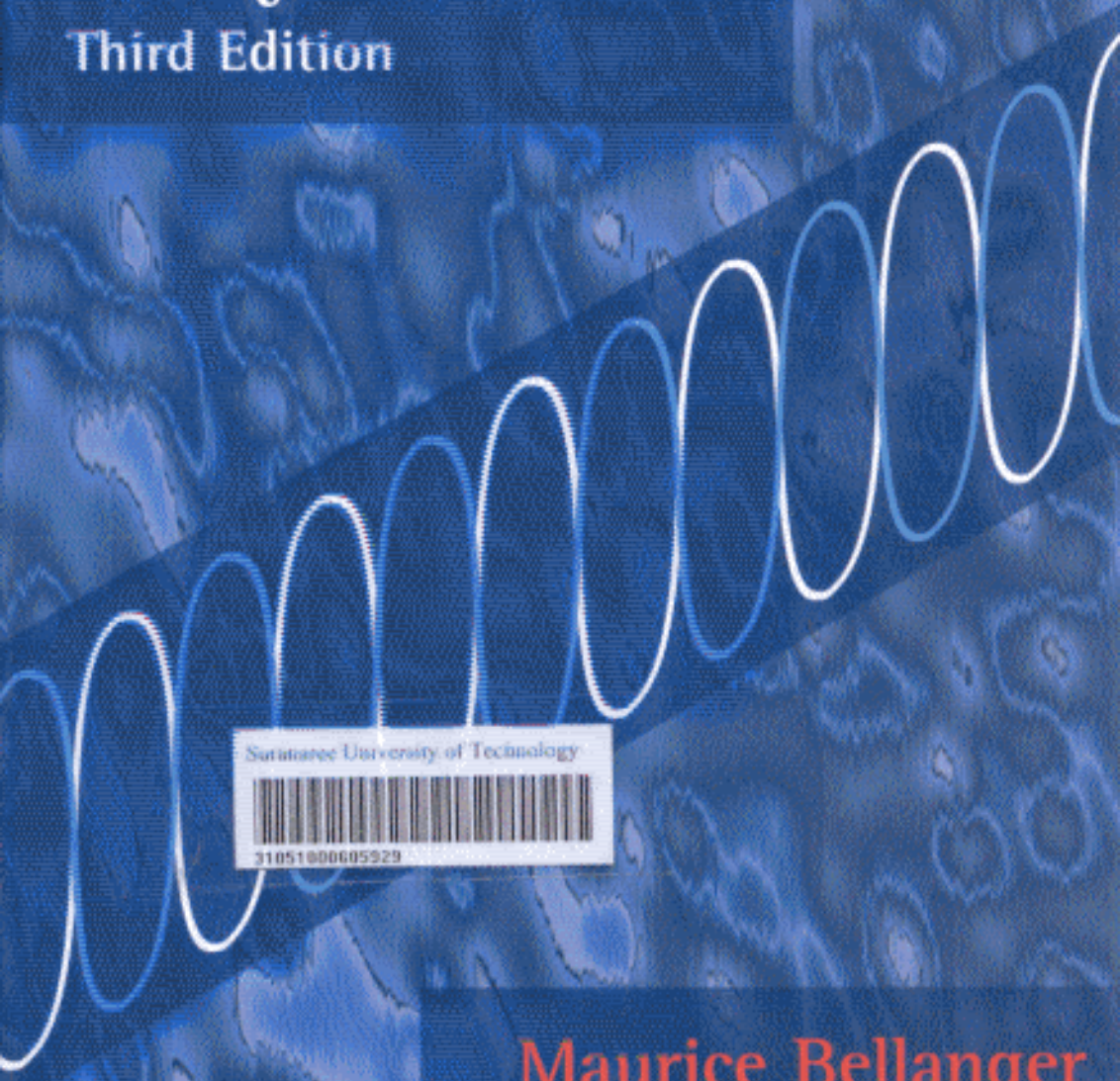
Digital Processing of Signals

Theory and Practice

Third Edition



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