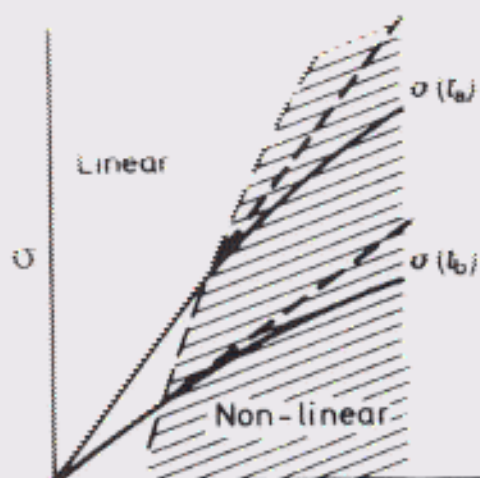


POLYMER VISCOELASTICITY

STRESS AND STRAIN IN PRACTICE



Suranaree University of Technology



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EVARISTO RIANDE
RICARDO DÍAZ-CALLEJA
MARGARITA G. PROLONGO
ROSA M. MASEGOSA
CATALINA SALOM

Contents

Preface	iii
1 Structure of Polymers	1
1.1 Introduction: Types of Polymers and Classification	1
1.2 Polymerization Processes	7
1.3 Molecular Weight and Molecular Weight Distribution	10
1.4 Configuration in Polymers	13
1.5 Conformational States in Polymers	16
1.6 Statistical Coil	18
Problem Sets	25
References	28
2 Crystalline and Amorphous States in Polymers	29
2.1 Introduction: Crystalline and Amorphous Regions in Polymers	29
2.2 Factors Determining the Crystallinity of Polymers	32
2.3 Crystal Structures of Polymers	33
2.4 Crystalline Morphology	37
2.5 Crystallization	43
2.6 Melting	46
2.7 Polymers in the Liquid Crystal State	51
2.8 Glassy State	57
2.9 Phenomenology of the Glass Transition	58
	vii

2.10	Glass Transition and Free Volume	62
2.11	Factors Affecting the Glass Transition of Polymers	66
	Problem Sets	76
	References	83
3	Rubber Elasticity	85
3.1	Introduction	85
3.2	Thermodynamic Treatment	88
3.3	Statistical Treatment	93
3.4	Modifications to Simple Statistical Theory—Non-Gaussian Statistics	106
3.5	Swelling of Polymer Networks	109
3.6	Elastomers in Service	111
	Problem Sets	132
	References	139
4	Stress-Strain Relations for Ideal Solids and Ideal Liquids	140
4.1	Ideal Solids and Liquids: Constitutive Equations	140
4.2	Stress Tensor	143
4.3	The Second Law of Dynamics	146
4.4	Strain Tensor	147
4.5	Compatibility Equations	151
4.6	Effect of Symmetry on the Relationships Between the Stress and Strain Tensors in Ideal Elastic Systems	152
4.7	Generalized Stress-Strain Hooke's Law for Isotropic Solids	162
4.8	Navier Equations	167
4.9	Generalized Strain-Stress Relationships for Ideal Elastic Systems	170
4.10	Thermoelastic Effects	172
4.11	Viscosity of Ideal Liquids	175
	Problem Sets	177
	References	195
5	Linear Viscoelasticity and Viscoelastic Functions	196
5.1	Viscoelasticity	196
5.2	Linear Viscoelasticity—Response of Materials to Transient Experiments	198
5.3	Boltzmann Superposition Principle in Creep Experiments	207
5.4	Memory Effects in Creep Experiments	212
5.5	Boltzmann Superposition Principle in Relaxation Experiments	214

5.6	Memory Function in Relaxation Experiments	216
5.7	Ramp Experiments	217
5.8	Laplace Transform Relationships Between Transient Relaxation Moduli and Transient Compliance Functions	218
5.9	Generalization of the Superposition Principle	221
5.10	Generalized Stress-Strain Relationships in the Frequency Domain	226
5.11	Generalized Stress-Strain Relationships for Viscoelastic Systems with Any Degree of Symmetry	227
	Problem Sets	228
	References	237
6	Dynamic Viscoelastic Functions	238
6.1	Introduction	238
6.2	Dynamic Relaxation Functions	239
6.3	Transformation of Relaxation Functions from the Frequency Domain to the Time Domain and Vice Versa	242
6.4	Complex Viscosity	242
6.5	Dissipated Energy in Dynamic Relaxation Experiments	243
6.6	Dynamic Creep Compliance Functions	244
6.7	Transformation of Compliance Functions from the Frequency Domain to the Time Domain and Vice Versa for Viscoelastic Solids	245
6.8	Dissipated Energy in Dynamic Creep Experiments	249
6.9	Analysis of Complex Creep Compliance Functions at Low Frequencies	250
6.10	Zero Shear Rate Viscosity and Steady-State Compliance Expressed in Terms of Viscoelastic Functions	252
6.11	Krönig-Kramers Relationships	253
6.12	Other Dynamic Viscoelastic Functions	255
	Problem Sets	257
	References	270
7	Experimental Determination of Viscoelastic Properties	271
7.1	Introduction	272
7.2	Experimental Determination of Dynamic Viscoelastic Properties	273
7.3	Torsion Pendulum	274
7.4	Corrections in the Determination of $G^*(\omega)$ from Free Oscillations in Shear	279
7.5	Forced Oscillations	280

7.6	Secondary Effects in Torsion	280
7.7	Effective Sample Length	283
7.8	Dynamic Mechanical Analysis by Transverse Flexion	285
7.9	Response of a Viscoelastic Rod to an Instantaneous Stimulus (Free Oscillations)	290
7.10	Determination of the Corrections in the Viscoelastic Functions Due to Clamping	292
7.11	Resonance Instruments	294
7.12	Wave Propagation	294
7.13	Experimental Determination of Static Viscoelastic Properties	296
7.14	Torsional Creep	296
7.15	Tensile Creep	298
7.16	Stress Relaxation	299
	Problem Sets	300
	References	304
8	Viscoelastic Behavior of Polymers Above T_g	306
8.1	Time-Temperature Correspondence Principle	306
8.2	Prediction of the Shift Factors for Viscoelastic Liquids	321
8.3	Prediction of the Shift Factors for Viscoelastic Solids	322
8.4	Influence of Temperature on Horizontal Shift Factors	323
8.5	Effect of Pressure on the Viscoelastic Response	327
8.6	Differentiation of Regions in the Master Curves of the Viscoelastic Functions	327
8.7	Influence of Diluents on the Viscoelastic Behavior of Polymers	339
8.8	Effects of Cross-Linking on the Viscoelastic Functions	343
	Problem Sets	348
	References	357
9	Retardation and Relaxation Spectra	359
9.1	Introduction	359
9.2	Formulation of Transient and Nontransient Relaxation Moduli in Terms of Retardation Spectra	360
9.3	Formulation of Transient and Nontransient Compliance Functions in Terms of Retardation Spectra	362
9.4	Important Inequalities Among Viscoelastic Functions	365
9.5	Determination of Viscosity and Steady-State (Equilibrium) Compliance from Relaxation and Retardation Spectra	366
9.6	Comparison of Retardation and Relaxation Times	368

9.7	Determination of Spectra from Viscoelastic Functions Using First-Order Approximations	371
9.8	Approximations of Higher Order	375
9.9	Experimental Retardation and Relaxation Spectra	378
9.10	Approximate Relationships Between Viscoelastic Functions	383
	Problem Sets	384
	References	393
10	Viscoelastic Models	394
10.1	Introduction	394
10.2	Maxwell's Model	395
10.3	The Kelvin-Voigt Model	398
10.4	Three-Element Standard Solid	400
10.5	Burgers Model	404
10.6	Maxwell and Kelvin-Voigt Generalized Models	406
10.7	Ladder Models	408
10.8	Distributed Constants Models	409
	Problem Sets	413
	References	422
11	Molecular Models of Viscoelastic Polymers	423
11.1	Concentration Regimes	423
11.2	Isolated Chains as Hookean Elements	425
11.3	Spring-Bead Model: Rouse Theory	425
11.4	Spring-Bead Model: Zimm Theory	428
11.5	Tube Model	430
11.6	Polydispersity and the Tube Model	434
11.7	Rouse Dynamics: Viscosity and Steady-State Compliance for Low Molecular Weight Chains in the Melt	434
11.8	Reptation Dynamics: Viscosity and Steady-State Compliance for High Molecular Weight Chains in the Melt	436
11.9	Comparison of Theoretical and Experimental Viscoelastic Results	439
11.10	Friction Coefficient	440
11.11	Concentration Dependence of Viscoelastic Functions in the Semidilute and Concentrated Regimes	443
11.12	Branched Polymers	446
	Problem Sets	447
	References	452

12 Viscoelasticity of Glassy and Semicrystalline Polymers	454
12.1 General Considerations	454
12.2 Relaxations in the Frequency Domain at Temperatures Slightly Higher than T_g	457
12.3 Topology of the Dynamics in the Vicinity of the Glass-Transition Temperature	460
12.4 Viscoelastic Functions for Glassy Systems in the Frequency Domain	463
12.5 Dispersions in the Glassy State and the Glass Transition	464
12.6 Molecular Cooperativity in the Glass Transition	468
12.7 Structural Recovery in the Glassy State: Aging	473
12.8 Memory Effects and Physical Aging	474
12.9 Influence of Physical Aging on the Viscoelastic Functions: Time-Aging Time Correspondence Principle	478
12.10 Nonlinear Behavior in Aging	482
12.11 Final Remarks on Aging Processes	483
12.12 Relaxation Behavior of Semicrystalline Polymers: General Considerations	485
12.13 General Features of Crystalline Polymers	494
12.14 Time-Temperature Correspondence Principle	496
12.15 Modeling the Viscoelastic Behavior of Crystalline Polymers	496
Problem Sets	498
References	507
 13 Flow Behavior of Polymer Melts and Solutions	 509
13.1 Introduction	510
13.2 Constitutive Equations	510
13.3 Second-Order Fluids in Simple Shearing Flow	515
13.4 Normal Stresses	517
13.5 Rheometry	518
13.6 Intrinsic Viscosity of Polymers	524
13.7 Flow Through a Slit	529
13.8 Sources of Error in Capillary and Slit Flows	531
13.9 Coaxial Cylinder: Couette Flow	536
13.10 Cone-Plate Viscometers	539
13.11 Plate-Plate Viscometers	541
13.12 Experimental Determination of Normal Stresses. Coaxial Cylinders	542
13.13 Factors Governing the Non-Newtonian Behavior of Polymers	546
13.14 Non-Newtonian Viscosity Models	550
13.15 Cox-Merz Rule	552

13.16	Influence of Diluents and Plasticizers, Blends, and Fillers on Flow	553
13.17	Parameters Influencing the First Normal Stress Difference	557
13.18	Die Swelling	558
13.19	Melt Index	560
13.20	Thixotropy and Rheopexy	562
13.21	Stretching Flow	563
	Problem Sets	568
	References	579
14	Yield Crazing and Fracture	582
14.1	Introduction: Ductile and Brittle Behavior	582
14.2	Shear Yield	584
14.3	Crazing	602
14.4	Fracture in Polymers	613
	Problem Sets	642
	References	651
15	Reinforced Polymers	653
15.1	Introduction	653
15.2	Polymer Matrices	655
15.3	Reinforcements: Fibers	664
15.4	Properties of Reinforced Polymers	670
15.5	Mechanical Properties of Unidirectional Composites	672
15.6	Laminates	681
15.7	Short Fiber Composites	684
	Problem Sets	690
	References	695
16	Multiaxial Analysis of Linear Viscoelastic Stress	696
16.1	Introduction	697
16.2	Integral Formulation of Viscoelastic Problems	697
16.3	Differential Form for the Constitutive Stress-Strain Relationship	701
16.4	Constitutive Equations in Differential Form for Multiaxial Tension States	703
16.5	Thermoviscoelasticity	706
16.6	Special Problems in Structural Linear Viscoelasticity	708
16.7	Formulation and Classification of the Boundary Problems in Viscoelasticity	708

16.8	Applicability of the Correspondence Principle. Quasi-Static and Dynamic Problems	709
16.9	Superposition and Saint Venant Principles	710
16.10	Problems with Special Symmetries	710
16.11	The Dynamic Problem	716
16.12	Plane Strain Problems	721
16.13	Plane Stress Problems	727
16.14	Indentation and Impact Problems	735
16.15	Roller Ball Indentation	740
16.16	Wave Propagation in Viscoelastic Materials	748
	Problem Sets	754
	References	767
17	Flexion and Torsion of Viscoelastic Beams and Rods	769
17.1	Introduction	770
17.2	Beam Bending: Preliminary Hypotheses and Stress Tensor	770
17.3	Bending Moment	772
17.4	Radius of Curvature	772
17.5	Momentum and Force Balances in Beams	775
17.6	Indentation of a Clamped Beam	776
17.7	Shear Stress Analysis in Elastic Beams	779
17.8	Shear Strain Analysis	783
17.9	Viscoelastic Beams	788
17.10	Transverse Vibrations in Viscoelastic Beams	789
17.11	Thermal Effects on Transverse Vibrations	808
17.12	Torsion of Viscoelastic Rods	816
17.13	Displacement and Strain Tensor in Torsion	816
17.14	Stress Tensor in Torsion	818
17.15	Equilibrium Equations for Torsion	819
17.16	Boundary Conditions	820
17.17	Torsion Function Found by Separation of Variables	821
17.18	Moment of Torque	822
17.19	Motion and Boundary Condition Equations	824
17.20	Analysis of Torsional Oscillations Using an Elastic Auxiliary Element	832
	Problem Sets	836
	References	864
Appendix		866
A.1	Laplace Transformation	866
A.2	Properties of the Laplace Transformation	867

Contents

xv

A.3	Inverse of the Laplace Transformation	867
A.4	Carson Transformation	868
A.5	Fourier Transformation	868
A.6	Stieltjes Transformation	869
A.7	Table of Laplace Transformations	869
A.8	Reference	869

Index

871