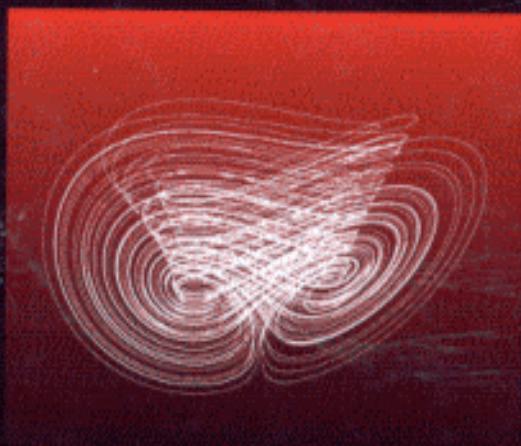


edited by  
Guanrong Chen



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**Controlling Chaos  
and Bifurcations  
in  
Engineering Systems**

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Suranaree University of Technology



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