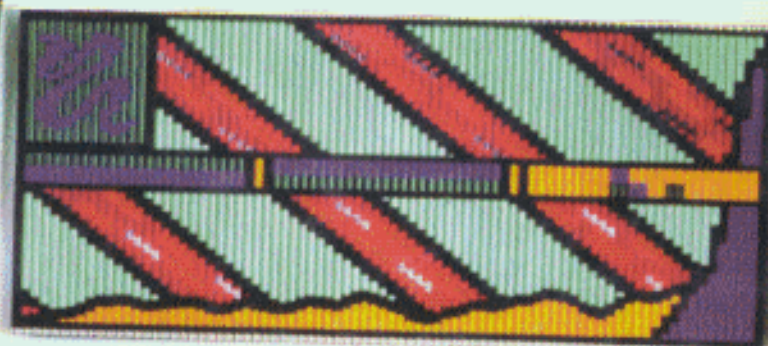


ELEMENTARY LINEAR ALGEBRA

A MATRIX APPROACH



SPENCE

Suranaree University of Technology



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