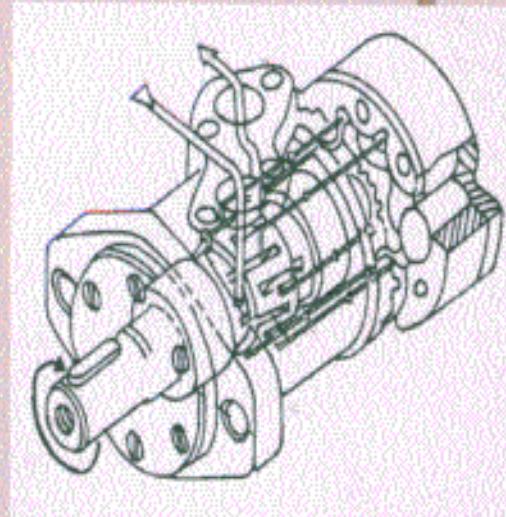
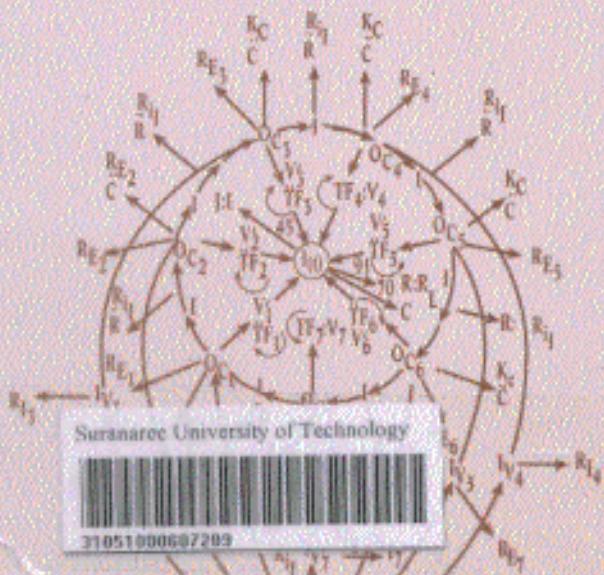


Modelling and Simulation of Engineering Systems through Bondgraphs




Narosa

$$\begin{array}{c} \text{C} \\ \text{Kp} \end{array} \xleftarrow{10p} \begin{array}{c} \text{R} \\ \text{R}_{pl} \end{array}$$

SI/VA

Amalendu Mukherjee
Ranjit Karmakar

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