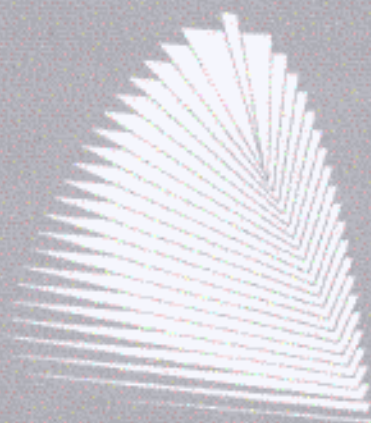


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STRUCTURE AND SYNTHESIS OF PID CONTROLLERS



Advances in
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