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Digital Diffractive Optics

**An Introduction to
Planar Diffractive Optics
and Related Technology**

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