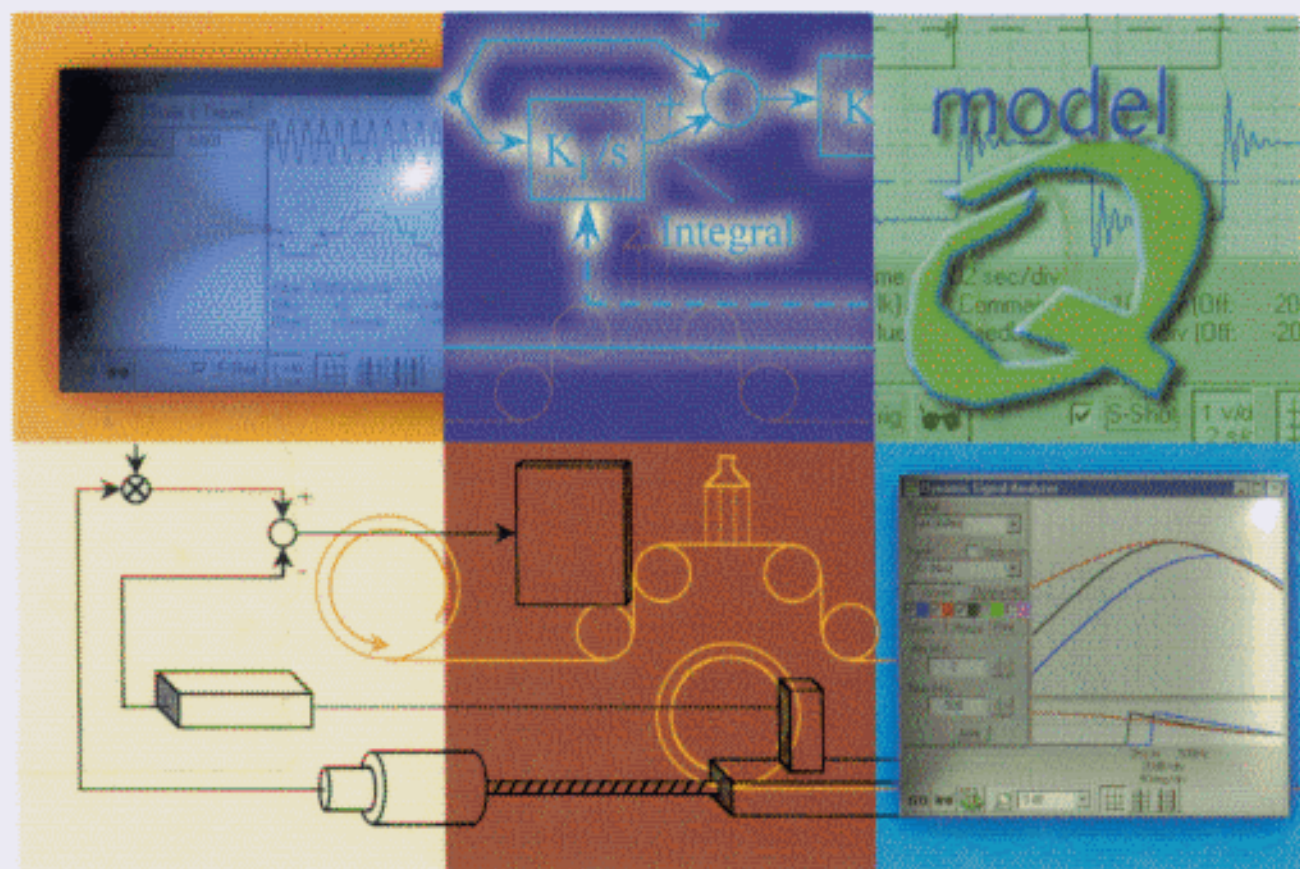


second edition

control system design guide

using your computer to understand
and diagnose feedback controllers



George Ellis

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