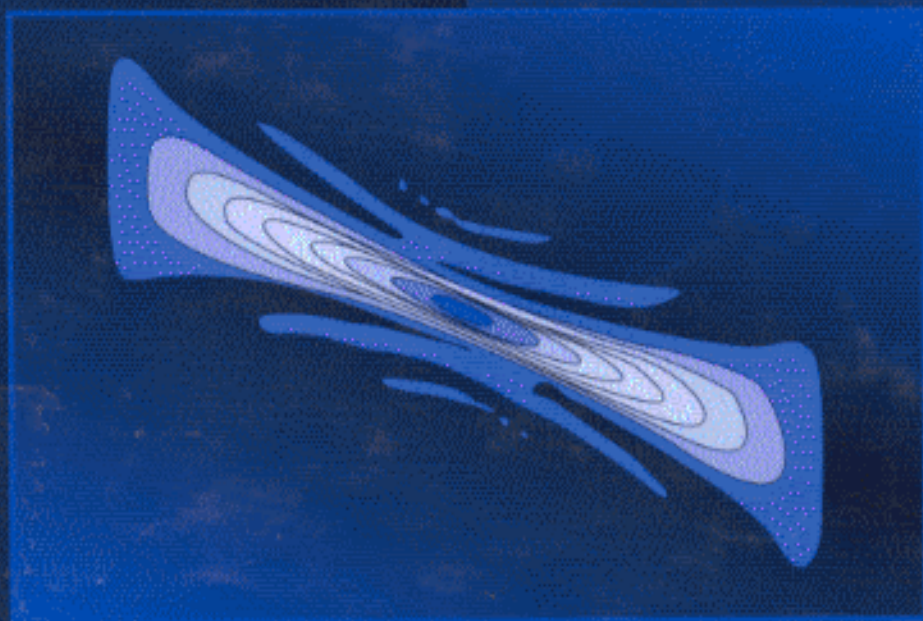


Radar Systems Analysis *and* Design *Using* **MATLAB**



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