NEW APPROACHES TO FUZZY MODELING AND CONTROL

DESIGN AND ANALYSIS

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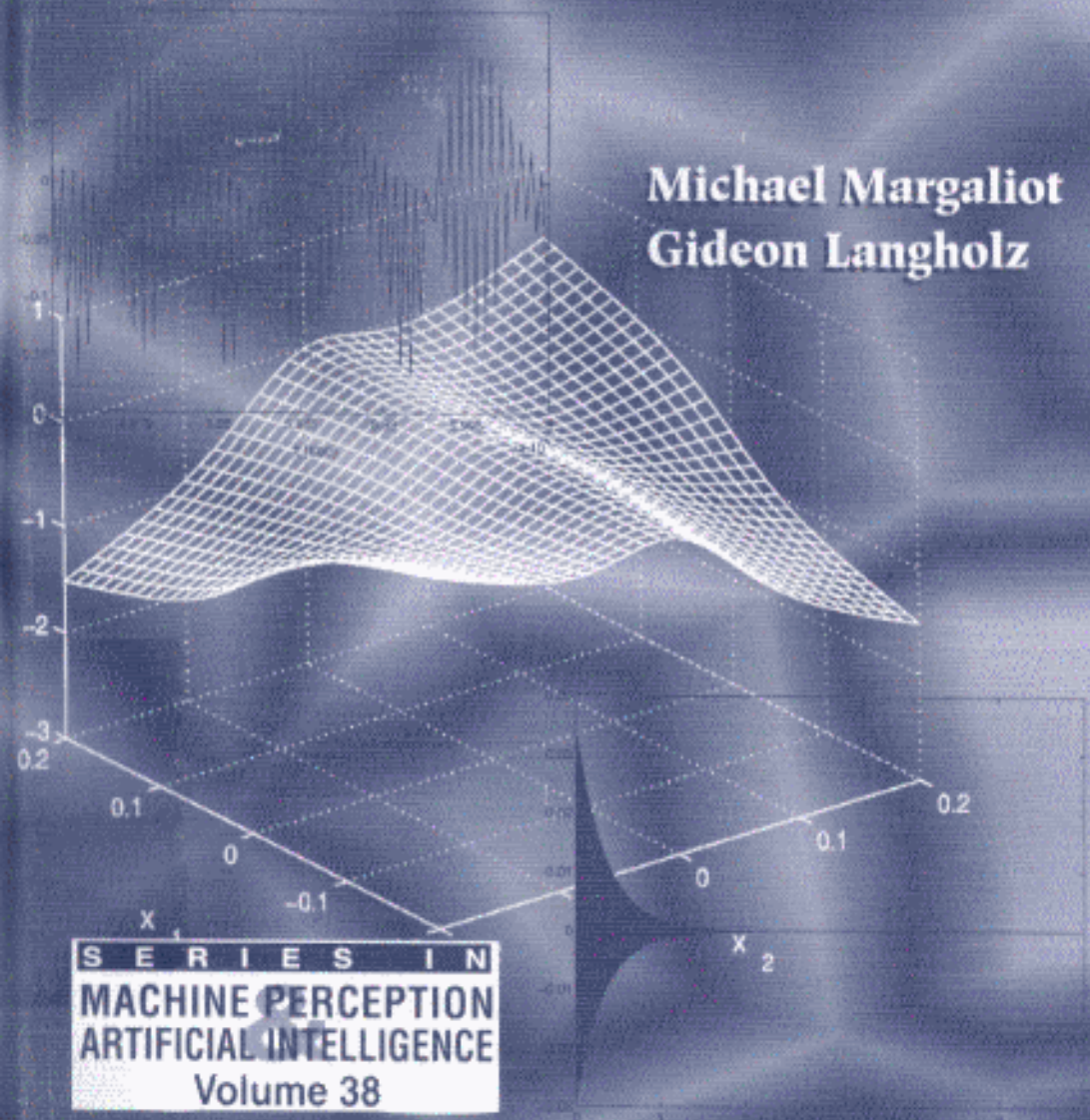

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