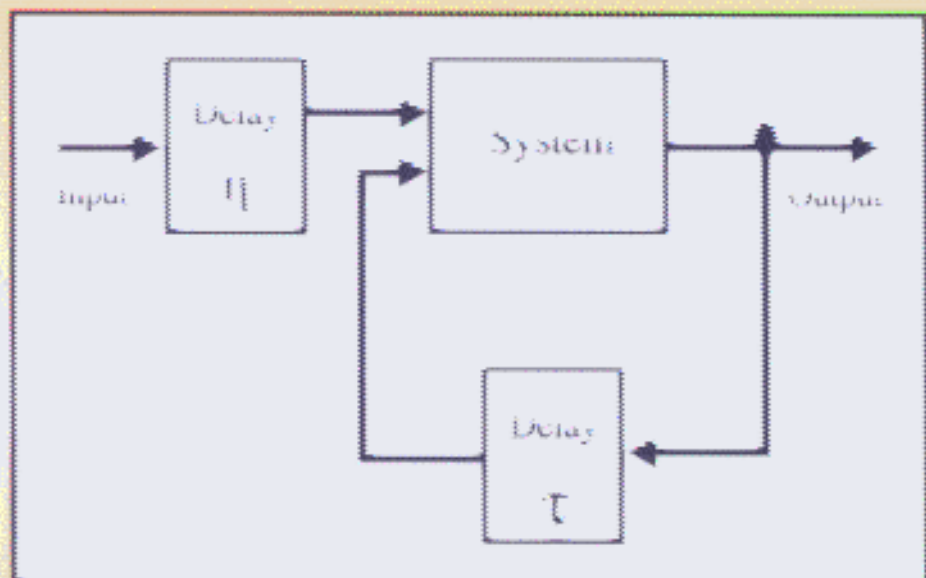


Control Engineering Series

ROBUST CONTROL AND FILTERING FOR TIME-DELAY SYSTEMS



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