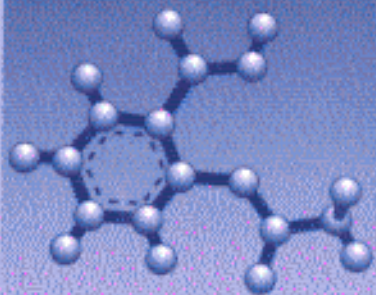


SPECIALIST PERIODICAL
REPORTS

RS•C
ROYAL SOCIETY OF CHEMISTRY



Chemical Modelling
APPLICATIONS AND THEORY

Volume 1

senior reporter A. HINCHLIFFE

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