

COMBINATORIAL OPTIMIZATION

# **Nonlinear Assignment Problems**

**Algorithms and Applications**

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