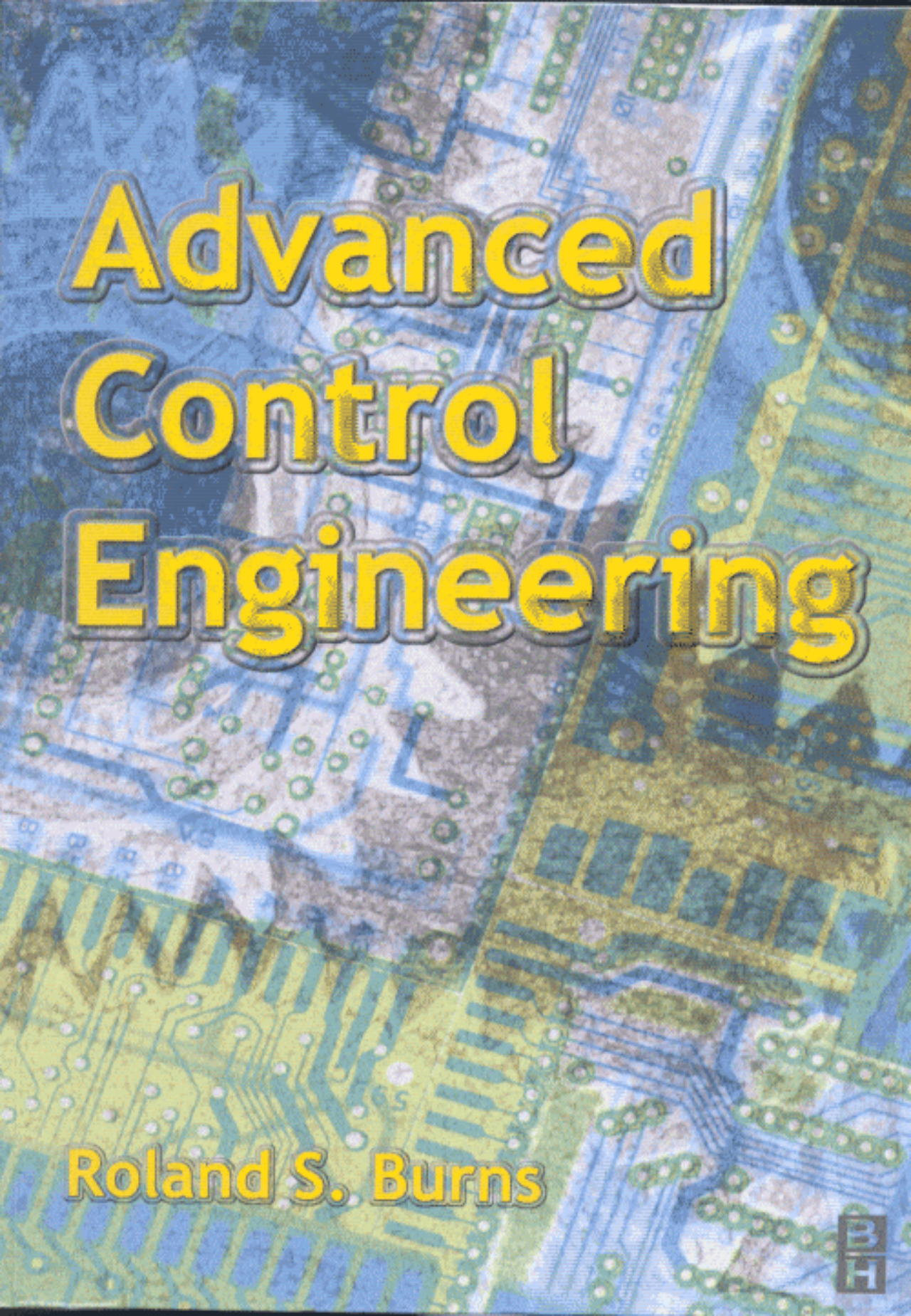
Advanced
Control
Engineering
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BH

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