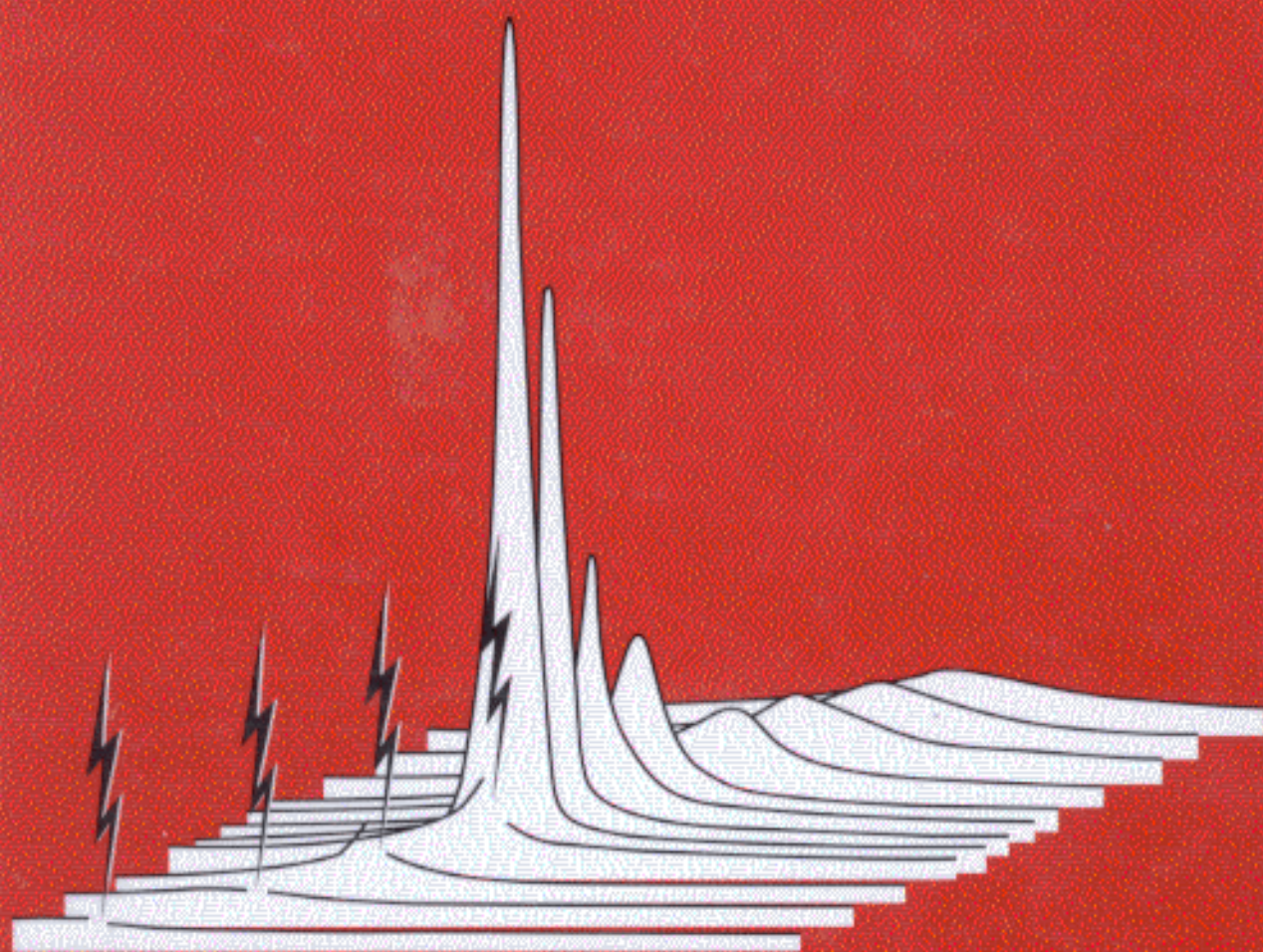


THE PHYSICAL BASIS OF THERMODYNAMICS

With Applications to Chemistry



Pascal Richet

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