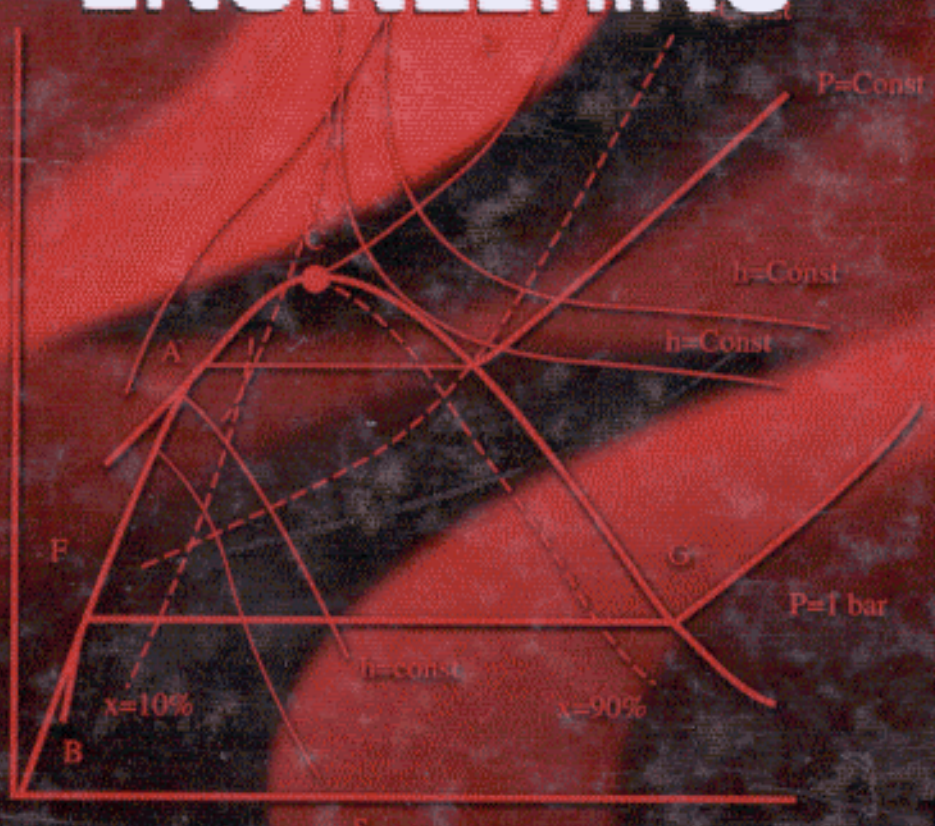
CRC Series in
COMPUTATIONAL MECHANICS and APPLIED ANALYSIS

ADVANCED THERMODYNAMICS ENGINEERING



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