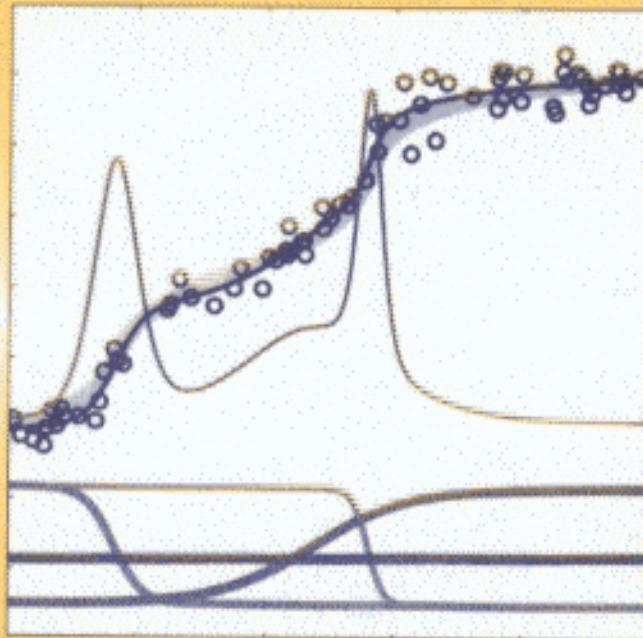


**Control Engineering Series**

# **ADVANCED PROCESS IDENTIFICATION AND CONTROL**



**Enso Ikonen  
Kaddour Najim**

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