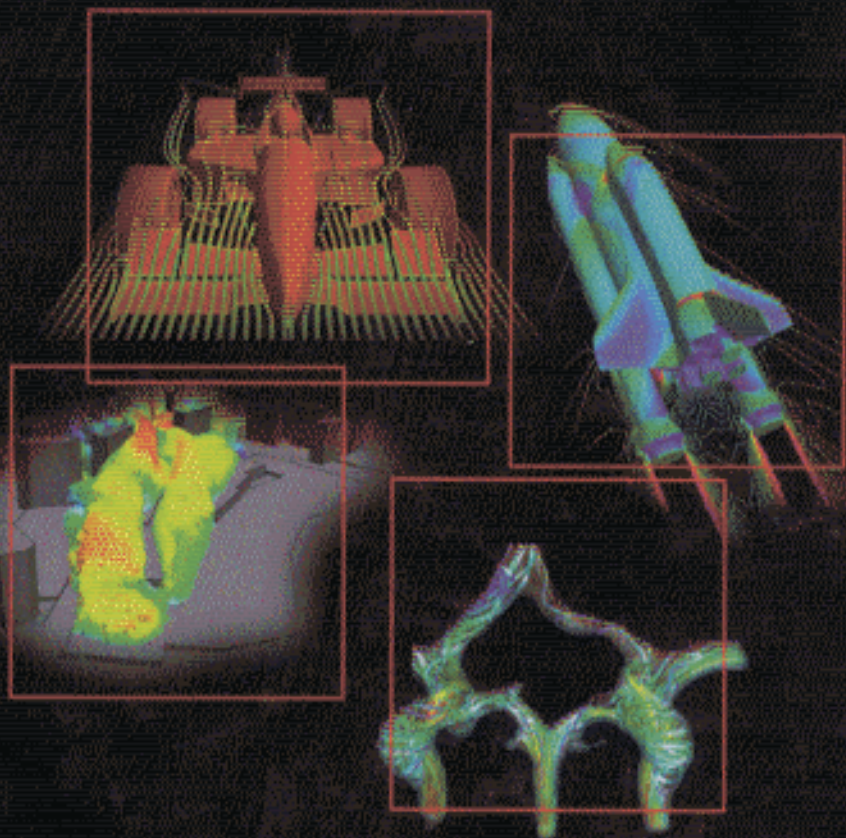


Applied CFD Techniques

An Introduction based on
Finite Element Methods



 WILEY

Rainald Löhner

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