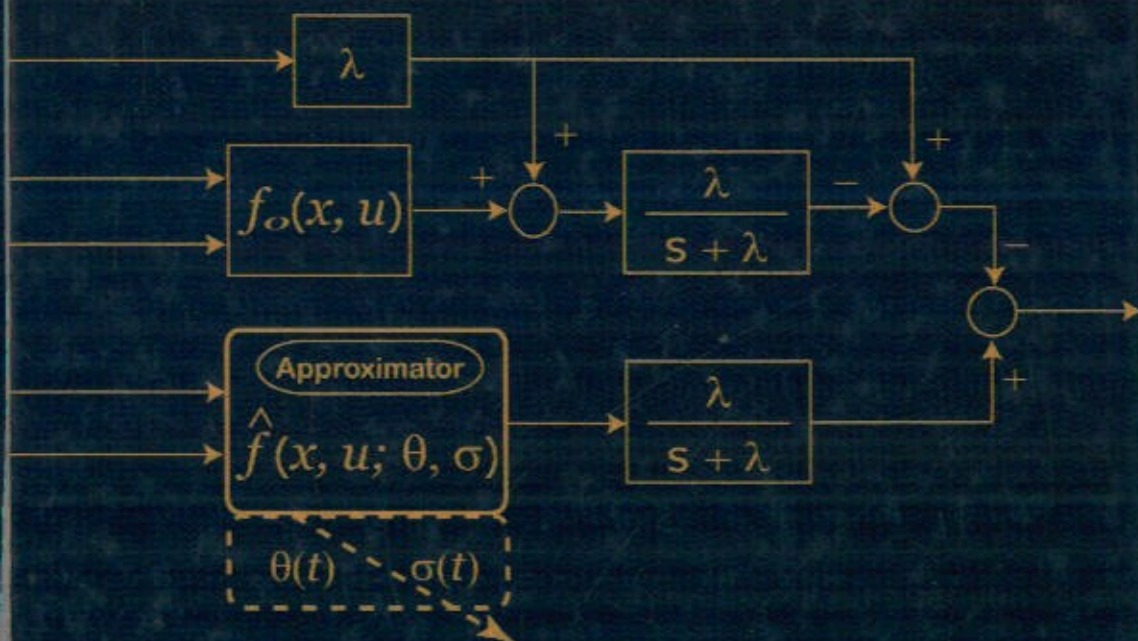


Adaptive Approximation Based Control

Unifying Neural, Fuzzy and Traditional Adaptive Approximation Approaches

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