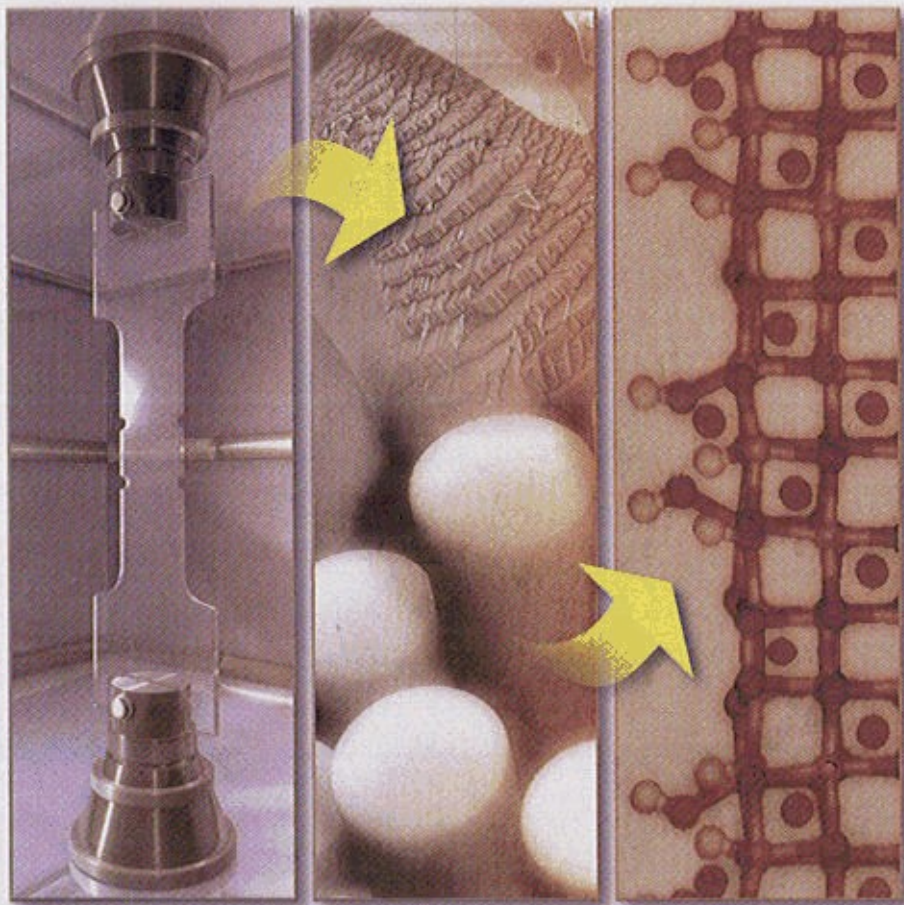


Gijsbertus de With

WILEY-VCH

Structure, Deformation, and Integrity of Materials

Volume I: Fundamentals and Elasticity



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