Six Sigma Operational Methods

DESIGN FOR SIX SIGMA STATISTICS

59 Tools for Diagnosing and Solving Problems in DFSS Initiatives

- Measurement System Analysis
- Process Capability Analysis
- Statistical Tools for Non-Normal Distributions

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