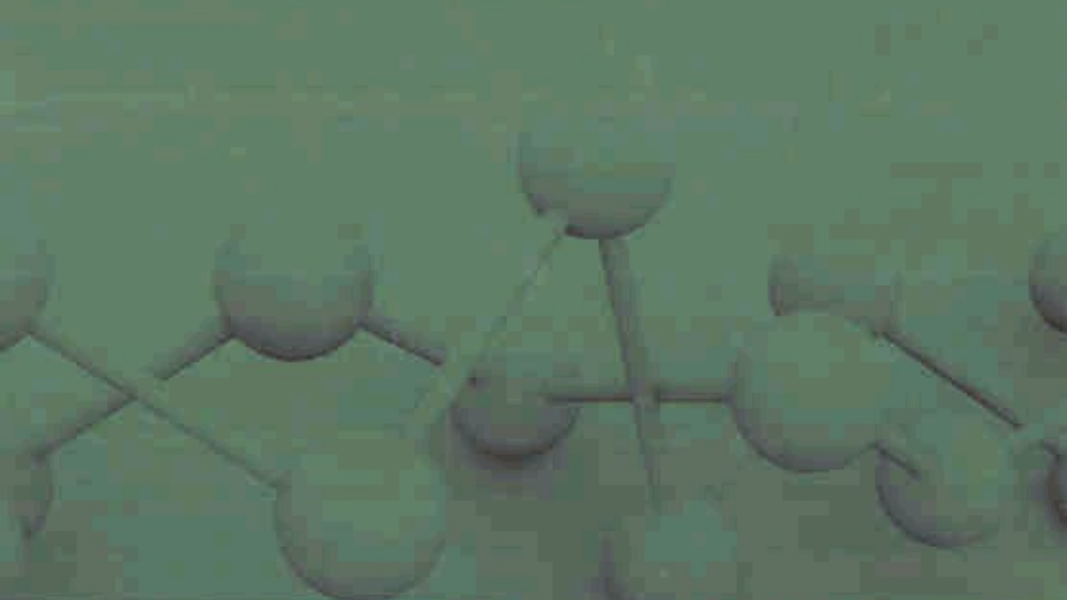


FUNDAMENTALS OF NATURAL COMPUTING

Basic Concepts, Algorithms, and Applications



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Chapman & Hall/CRC
Taylor & Francis Group

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