



SECOND EDITION

**Applied  
Numerical  
Methods  
with MATLAB**  
for Engineers and Scientists

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McGRAW·HILL INTERNATIONAL EDITION



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