

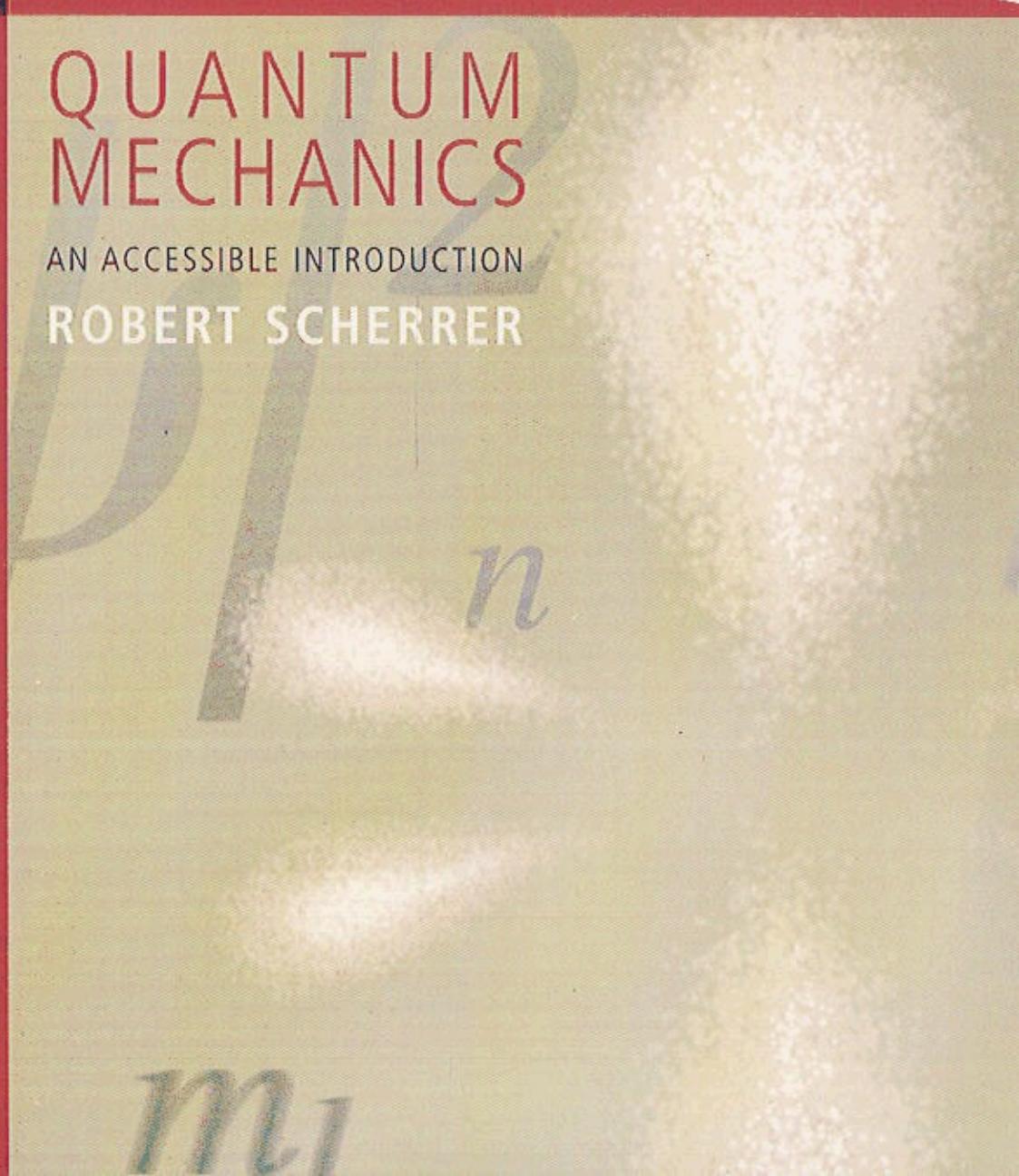


Pearson International Edition

QUANTUM MECHANICS

AN ACCESSIBLE INTRODUCTION

ROBERT SCHERRER



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