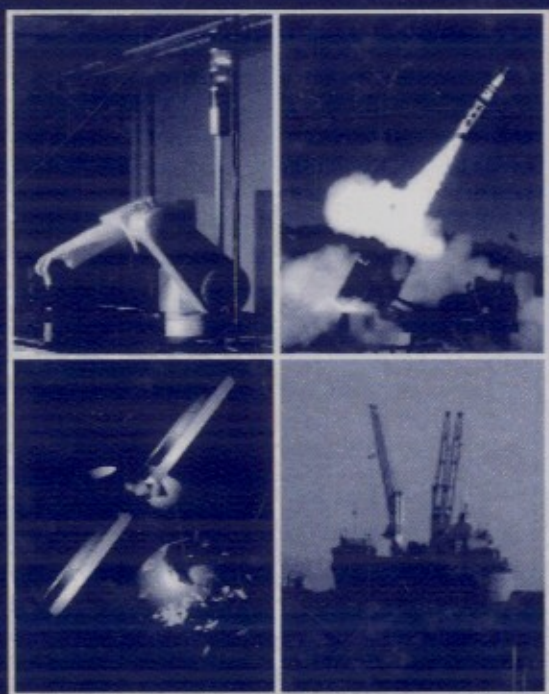


Applied Dynamic Programming for Optimization of Dynamical Systems



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Advances in Design and Control

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Contents

List of Figures	ix
List of Tables	xiii
Preface	xv
1 Introduction	1
1.1 Key Role of Dynamic Programming in Control Design	1
1.2 Illustrative Applications	2
1.3 Summary	7
2 Constrained Optimization	9
2.1 Introduction	9
2.1.1 Nomenclature for Iterative Optimization Methods	9
2.2 Unconstrained Optimization—The Descent Property	10
2.3 Including the Constraints	13
2.3.1 Equality Constraints	13
2.3.2 Inequality Constraints and the Karush–Kuhn–Tucker Conditions	14
2.4 Improving the Search with Second-Order Methods	16
2.4.1 Newton’s Method	16
2.4.2 Updating the Hessian for Curvature Input	17
2.5 The Quadratic Programming Problem	19
2.5.1 Solving the Linear System of Unknowns	19
2.5.2 A Merit Function for One-Dimensional Search	21
2.5.3 A Measure of Convergence and the Recursive Quadratic Programming Algorithm	21
2.6 Applications of Constrained Minimization	23
2.6.1 Implementation of the Recursive Quadratic Programming Algorithm	23
2.6.2 Optimizing Efficiencies in the Laser Welding Process	24
2.6.3 Maximum Terminal Velocity for Hypersonic Standoff Missiles	29

2.6.4	Optimal Slew Maneuvers for Space Telescope Attitude Control	37
2.7	Summary	42
3	Introduction to Dynamic Programming	45
3.1	Introduction	45
3.2	Discrete Dynamic Programming	45
3.2.1	Application of Discrete Dynamic Programming to Data Smoothing	47
3.2.2	Application of Discrete Dynamic Programming to Discrete-Time Optimal Control Problems	50
3.2.3	Implementation Details	52
3.3	A Nonlinear Optimal Control Problem with Constraints	57
3.4	Summary	65
4	Advanced Dynamic Programming	67
4.1	Introduction	67
4.2	A Dynamic Programming Approach to Rocket Guidance Problems . .	67
4.2.1	Physical Model	69
4.2.2	Guidance Problem	70
4.2.3	Transformation of the Guidance Problem	72
4.2.4	Dynamic Programming Solution	74
4.2.5	Numerical Simulation Results	75
4.3	Sequential Quadratic Programming Implementations for Equality-Constrained Optimal Control	77
4.3.1	Fixed Final Time Problems	77
4.3.2	Derivation of Recursive Equations	81
4.3.3	Constraint Equations	83
4.3.4	Algorithm for P1	84
4.3.5	Free Final Time Problems	85
4.3.6	Algorithm for P2	86
4.3.7	Practical Issues	86
4.3.8	Example Problems	87
4.4	A Dynamic Programming Method for Constrained Optimal Control . .	96
4.4.1	Problem Formulation	97
4.4.2	Sequential Quadratic Programming Subproblem Formulation	98
4.4.3	Interior Point Methods	100
4.4.4	Equivalent Problem Formulation	102
4.4.5	Details of Algorithm	105
4.4.6	Example Problems	108
4.5	Summary	114
5	Applied Case Studies	117
5.1	Introduction	117
5.2	Case Study 1: Rotary Jib Crane	118

5.2.1	Introduction	118
5.2.2	Model Development	119
5.2.3	Optimization Designs	124
5.2.4	Implementation Issues	125
5.2.5	Numerical Simulation Results	126
5.2.6	Case Study 1 Discussion (Summary/Conclusions)	132
5.3	Case Study 2: Slewing Flexible Link	134
5.3.1	Introduction	134
5.3.2	Model Development	136
5.3.3	Optimization Feedforward Command Design	142
5.3.4	Implementation Issues	145
5.3.5	Numerical Simulation Results	146
5.3.6	Case Study 2 Discussion (Summary/Conclusions)	150
5.4	Case Study 3: Flexible Planar Arm	151
5.4.1	Introduction	151
5.4.2	Model Development	152
5.4.3	Dynamic Programming Optimization Design	162
5.4.4	Implementation Issues	163
5.4.5	Numerical Simulation Results	163
5.4.6	Case Study 3 Discussion (Summary/Conclusions)	167
5.5	Case Study 4: Minimum-Time Maneuvers of Rigid Systems	170
5.5.1	Introduction	170
5.5.2	The Classic Double Integrator Example	171
5.5.3	Three-Axis Maneuvers of a Symmetric Spacecraft	173
5.5.4	Case Study 4 Discussion (Summary/Conclusions)	177
5.6	Case Study 5: Maximum-Radius Orbit Transfer	177
5.6.1	Introduction	177
5.6.2	Dynamical Model	178
5.6.3	Solution Using Dynamic Programming/Interior Point	178
5.6.4	Case Study 5 Discussion (Summary/Conclusions)	179
5.7	Case Study 6: PUMA 560 Industrial Manipulator	180
5.7.1	Introduction	180
5.7.2	Model Development	180
5.7.3	Dynamic Programming Optimization Design	184
5.7.4	Implementation Issues	185
5.7.5	Numerical Simulation Results	186
5.7.6	Case Study 6 Discussion (Summary/Conclusions)	189
5.8	Summary	189
A	Mathematical Supplement	191
A.1	Determination of the State Transition Matrices	191
A.2	Example 4.3 Numerical Approach	192
A.3	Modified Dynamic Programming Algorithm	194
B	Applied Case Studies—MATLAB Software Addendum	197
B.1	Case Study 1 Driver Functions and Script Files	197

B.1.1	Rotary Jib Crane Numerical Simulations Code	197
B.1.2	Dynamic Programming/Interior-Point Driver, Cost, Equality, Inequality, and Dynamics Code	202
B.2	Case Study 2 Driver Functions and Script Files	205
B.2.1	Slewing Flexible Link Numerical Simulations Code	205
B.2.2	Dynamic Programming/Interior-Point Driver, Cost, Equality, Inequality, and Dynamics Code	209
B.2.3	<i>fmincon</i> Driver, Cost, Constraints, and Dynamics Code	215
B.3	Case Study 3 Driver Functions and Script Files	219
B.3.1	Dynamic Programming/Interior-Point Driver, Cost, Equality, Inequality, and Dynamics Code	219
B.4	Case Study 4 Driver Functions and Script Files	225
B.4.1	Dynamic Programming/Interior-Point Driver, Cost, Equality, Inequality, and Dynamics Code	225
B.5	Case Study 5 Driver Functions and Script Files	229
B.5.1	Dynamic Programming/Interior-Point Driver, Cost, Equality, Inequality, and Dynamics Code	229
B.6	Case Study 6 Driver Functions and Script Files	233
B.6.1	Dynamic Programming/Interior-Point Driver, Cost, Equality, Inequality, and Dynamics Code	233
B.6.2	PUMA560 Dynamic Equations of Motion C-Code	239
B.7	Discrete Dynamic Programming Standalone Code—Discrete-Time Optimal Control Problem	246

Bibliography	251
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Index	259
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