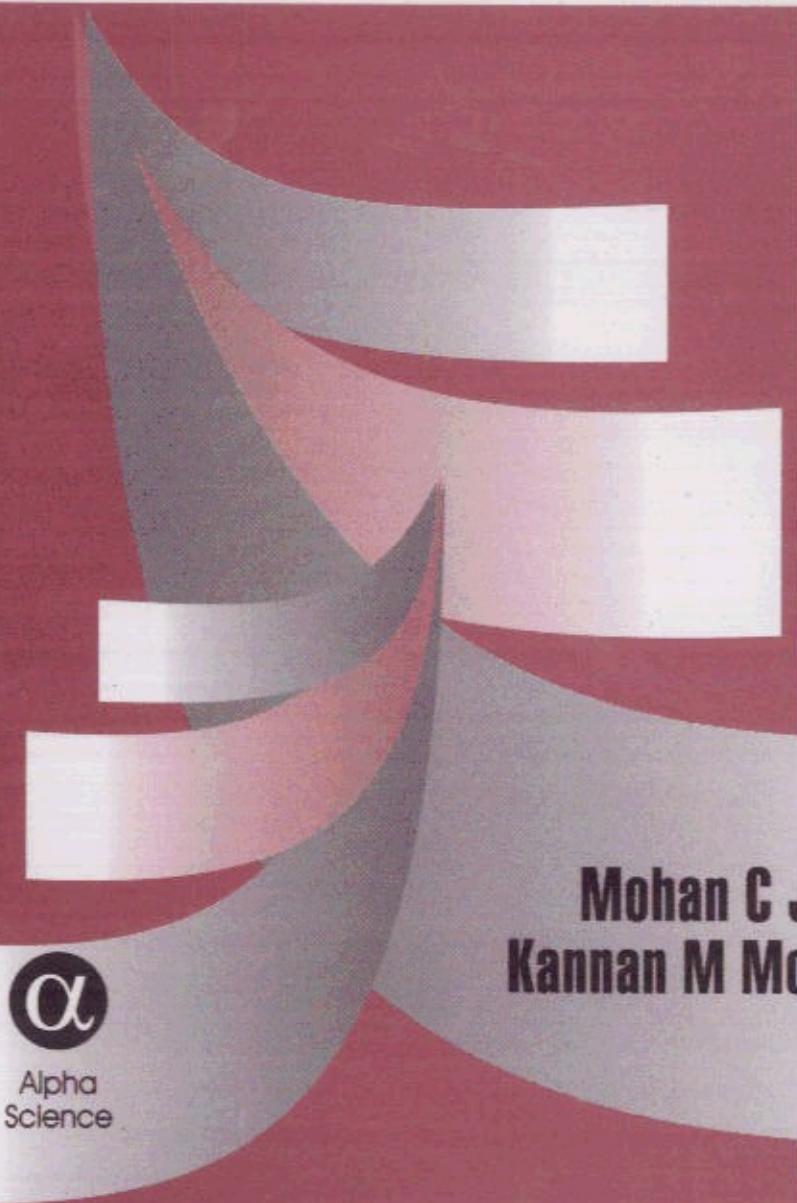


Optimization

Theory and Practice



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Alpha
Science

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