

Series on
Applied Mathematics
Volume 18

POOLING DESIGNS AND NONADAPTIVE GROUP TESTING

Important Tools for
DNA Sequencing

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World Scientific

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