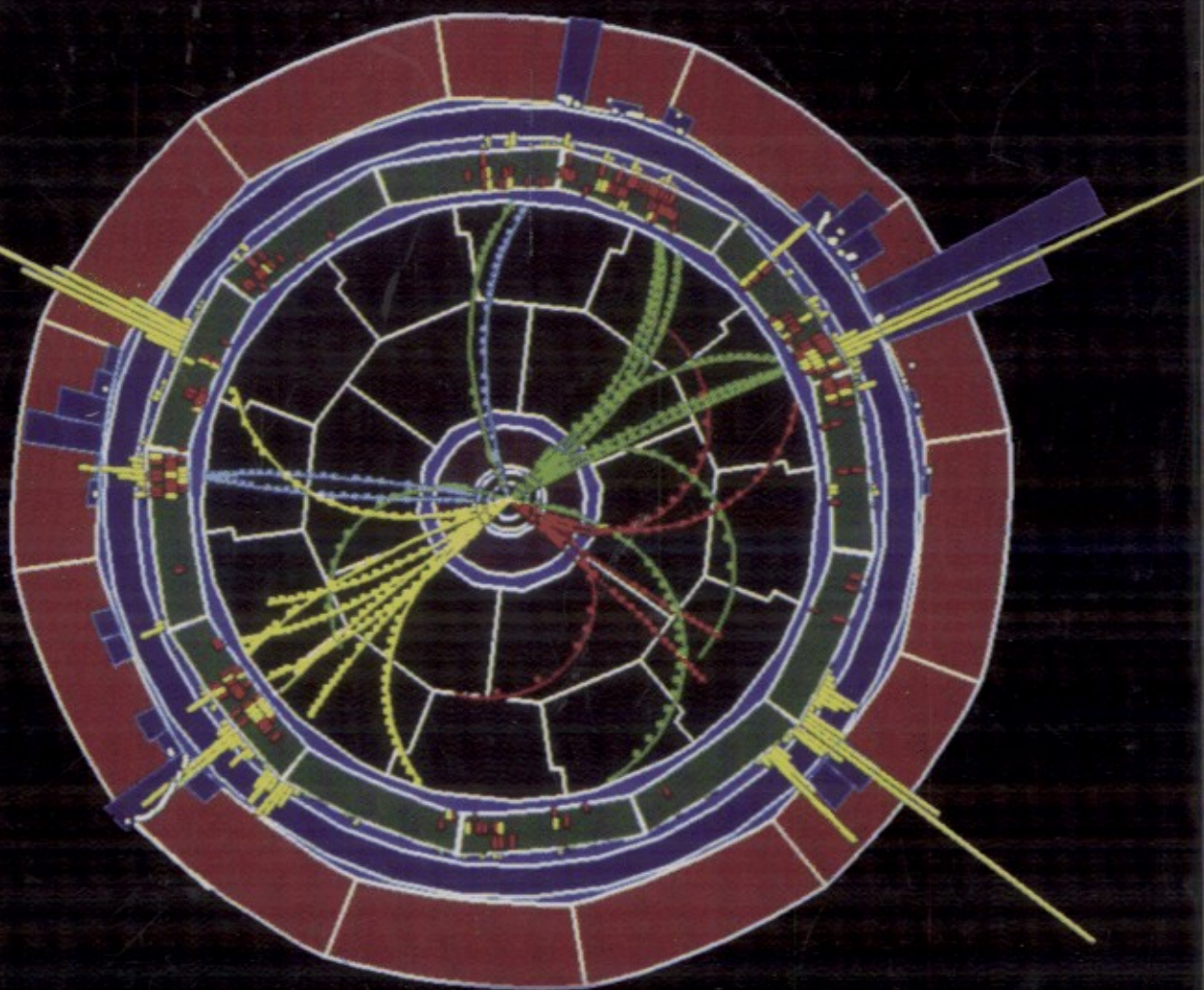


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An Introduction to the Standard Model of Particle Physics

Second Edition



CAMBRIDGE

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