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# The Finite Element Method and Applications in Engineering Using ANSYS<sup>®</sup>

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*includes CD-ROM*

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 Springer

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