

## Hydrosystems Engineering Reliability Assessment and Risk Analysis

- ✓ Safety and reliability in varying design scenarios
- ✓ Mathematical tools for solving hydrosystem engineering problems
- ✓ How to conduct risk and reliability assessments

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## **Contents**

## Preface xi Acknowledgments xv

| Chap  | er 1. Reliability in Hydrosystems Engineering                             | 1  |
|-------|---|----|
| 1.1   | Reliability Engineering   | 1  |
| 1.2   | Reliability of Hydrosystem Engineering Infrastructure                     | 2  |
| 1.3   | Brief History of Engineering Reliability Analysis                         | 6  |
| 1.4   | Concept of Reliability Engineering  | 7  |
|       | Definitions of Reliability and Risk                                       | 10 |
|       | Measures of Reliability   | 13 |
| 1.7   | •   | 15 |
|       | References  | 16 |
| Chapt | er 2. Fundamentals of Probability and Statistics for Reliability Analysis | 19 |
| 2.1   | Terminology   | 19 |
|       | Fundamental Rules of Probability Computations                             | 21 |
|       | 2.2.1 Basic axioms of probability   | 21 |
|       | 2.2.2 Statistical independence  | 22 |
|       | 2.2.3 Conditional probability   | 23 |
|       | 2.2.4 Total probability theorem and Bayes' theorem                        | 24 |
| 2.3   | Random Variables and their Distributions                                  | 27 |
|       | 2.3.1 Cumulative distribution function and probability density function   | 27 |
|       | 2.3.2 Joint, conditional, and marginal distributions                      | 31 |
| 2.4   | Statistical Properties of Random Variables                                | 35 |
|       | 2.4.1 Statistical moments of random variables                             | 35 |
|       | 2.4.2 Mean, mode, median, and quantiles                                   | 40 |
|       | 2.4.3 Variance, standard deviation, and coefficient of variation          | 43 |
|       | 2.4.4 Skewness coefficient and kurtosis                                   | 44 |
|       | 2.4.5 Covariance and correlation coefficient                              | 47 |
| 2.5   | Discrete Univariate Probability Distributions                             | 49 |
|       | 2.5.1 Binomial distribution   | 51 |
|       | 2.5.2 Poisson distribution  | 53 |
| 2.6   | Some Continuous Univariate Probability Distributions                      | 55 |
|       | 2.6.1 Normal (Gaussian) distribution                                      | 56 |
|       | 2.6.2 Lognormal distribution  | 60 |
|       | 2.6.3 Gamma distribution and variations                                   | 63 |

|        | 2.6.4 Extreme-value distributions  | 74         |
|--------|--|------------|
|        | 2.6.5 Beta distributions 2.6.6 Distributions related to normal random variables  | 71<br>72   |
| 27     | Multivariate Probability Distributions   | 75         |
| 2.7    | 2.7.1 Multivariate normal distributions  | 77         |
|        | 2.7.2 Computation of multivariate normal probability   | 81         |
|        | 2.7.3 Determination of bounds on multivariate normal probability   | 88         |
|        | 2.7.4 Multivariate lognormal distributions   | 91         |
|        | Problems   | 92         |
|        | References   | 101        |
|        |  |            |
| Chapte | er 3. Hydrologic Frequency Analysis  | 103        |
| 3.1    | Types of Geophysical Data Series   | 104        |
|        | Return Period  | 108        |
| 3.3    | Probability Estimates for Data Series: Plotting Positions (Rank-order Probability)   | 109        |
| 3.4    | Graphic Approach   | 111        |
| 3.5    | Analytical Approaches  | 114        |
| 3.6    | Estimation of Distributional Parameters  | 119        |
|        | 3.6.1 Maximum-likelihood (ML) method   | 119        |
|        | 3.6.2 Product-moments-based method   | 121        |
|        | 3.6.3 L-moments-based method   | 122        |
| 3.7    | Selection of Distribution Model  | 125        |
|        | 3.7.1 Probability plot correlation coefficients  | 125        |
|        | 3.7.2 Model reliability Indices  | 126        |
|        | 3.7.3 Moment-ratio diagrams  | 126        |
|        | 3.7.4 Summary  | 129        |
|        | Uncertainty Associated with a Frequency Relation   | 129        |
| 3.9    | Limitations of Hydrologic Frequency Analysis   | 135        |
|        | 3.9.1 Distribution selection: practical considerations   | 135<br>135 |
|        | 3.9.2 Extrapolation problems 3.9.3 The stationarity assumption   | 139        |
|        | 3.9.4 Summary comments   | 139        |
|        | Problems   | 140        |
|        | References   | 142        |
|        |  | ,          |
| Chapt  | er 4. Reliability Analysis Considering Load-Resistance Interference  | 145        |
|        | Basic Concept  | 145        |
| 4.2    | Performance Functions and Reliability Index  | 147        |
| 4.3    | Direct Integration Method  | 149        |
| 4.4    | Mean-Value First-Order Second-Moment (MFOSM) Method  | 156        |
| 4.5    | Advanced First-Order Second-Moment (AFOSM) Method  | 164        |
|        | 4.5.1 Definitions of stochastic parameter spaces   | 164        |
|        | 4.5.2 Determination of design point (most probable failure point)  | 165        |
|        | 4.5.3 First-order approximation of performance function at the design point  | 169        |
|        | 4.5.4 Algorithms of AFOSM for independent normal parameters 4.5.5 Treatment of nonnormal stochastic variables                            | 173<br>180 |
|        |  | 185        |
|        | 4.5.6 Treatment of correlated normal stochastic variables 4.5.7 AFOSM reliability analysis for nonnormal correlated stochastic variables | 190        |
|        | 4.5.8 Overall summary of AFOSM reliability method  | 200        |
| Λ¢     | Second-Order Reliability Methods   | 203        |
| 4.0    | 4.6.1 Quadratic approximations of the performance function   | 204        |
|        | 4.6.2 Breitung's formula   | 208        |

|       | Contents  | vii |
|-------|---|-----|
| 4.7   | Time-Dependent Reliability Models   | 211 |
|       | 4.7.1 Time-dependent resistance   | 213 |
|       | 4.7.2 Time-dependent load   | 214 |
|       | 4.7.3 Classification of time-dependent reliability models   | 214 |
|       | 4.7.4 Modeling intensity and occurrence of loads  | 215 |
|       | 4.7.5 Time-dependent reliability models   | 217 |
|       | 4.7.6 Time-dependent reliability models for hydrosystems  | 218 |
|       | Appendix 4A: Some One-Dimensional Numerical Integration Formulas  | 221 |
|       | Appendix 4B: Cholesky Decomposition   | 223 |
|       | Appendix 4C: Orthogonal Transformation Techniques   | 224 |
|       | Appendix 4D: Gram-Schmid Ortho Normalization  | 229 |
|       | Problems  | 231 |
|       | References  | 240 |
| Chapt | er 5. Time-to-Failure Analysis  | 245 |
| 5.1   | Pagia Canaant   | 245 |
|       | Basic Concept Failure Characteristics   | 246 |
| 5.2   | 5.2.1 Failure density function  | 246 |
|       | 5.2.2 Failure rate and hazard function  | 247 |
|       | 5.2.3 Cumulative hazard function and average failure rate   | 251 |
|       | 5.2.5 Typical hazard functions  | 254 |
|       | 5.2.6 Relationships among failure density function, failure rate, and reliability   | 255 |
|       | 5.2.7 Effect of age on reliability  | 257 |
|       | 5.2.8 Mean time to failure  | 259 |
| 5.3   | Repairable Systems  | 259 |
|       | 5.3.1 Repair density and repair probability   | 261 |
|       | 5.3.2 Repair rate and its relationship with repair density and repair probability 5.3.3 Mean time to repair, mean time between failures, and mean | 263 |
|       | time between repairs  | 263 |
|       | 5.3.4 Preventive maintenance  | 264 |
|       | 5.3.5 Supportability  | 272 |
| 5.4   | Determinations of Availability and Unavailability   | 272 |
|       | 5.4.1 Terminology   | 272 |
|       | 5.4.2 Determinations of availability and unavailability   | 275 |
|       | Appendix 5A: Laplace Transform  | 282 |
|       | Problems  | 283 |
|       | References  | 286 |
| Chapt | ter 6. Monte Carlo Simulation   | 289 |
| 6.1   | Introduction  | 289 |
|       | Generation of Random Numbers  | 291 |
|       | Classifications of Random Variates Generation Algorithms  | 294 |
| 0.0   | 6.3.1 CDF-inverse method  | 294 |
|       | 6.3.2 Acceptance-rejection methods  | 296 |
|       | 6.3.3 Variable transformation method  | 298 |
| 6.4   | Generation of Univariate Random Numbers for Some Distributions  | 299 |
|       | 6.4.1 Normal distribution   | 299 |
|       | 6.4.2 Lognormal distribution  | 301 |
|       | 6.4.3 Exponential distribution  | 301 |
|       | 6.4.4 Gamma distribution  | 302 |
|       | 6.4.5 Poisson distribution  | 302 |
|       | 6.4.6 Other univariate distributions and computer programs  | 303 |

| 6.5   | Generation of Vectors of Multivariate Handom Variables  | 303        |
|-------|---|------------|
|       | 6.5.1 CDF-inverse method  | 304        |
|       | 6.5.2 Generating multivariate normal random variates  | 307        |
|       | 6.5.3 Generating multivariate random variates with known marginal                                       |            |
|       | PDFs and correlations   | 311        |
|       | 6.5.4 Generating multivariate random variates subject to linear constraints                             | 312        |
| 6.6   | Monte Carlo Integration   | 314        |
|       | 6.6.1 The hit-and-miss method   | 316        |
|       | 6.6.2 The sample-mean method  | 319        |
|       | 6.6.3 Directional Monte Carlo simulation algorithm  | 321        |
|       | 6.6.4 Efficiency of the Monte Carlo algorithm   | 327        |
| 6.7   | Variance-Reduction Techniques   | 327        |
|       | 6.7.1 Importance sampling technique   | 328        |
|       | 6.7.2 Antithetic-variates technique   | 330        |
|       | 6.7.3 Correlated-sampling techniques  | 333        |
|       | 6.7.4 Stratified sampling technique   | 335        |
|       | 6.7.5 Latin hypercube sampling technique 6.7.6 Control-variate method                                   | 338<br>342 |
| 6.0   |   |            |
| 6.8   | Resampling Techniques   | 34         |
|       | Problems  | 348        |
|       | References  | 352        |
| Chapt | er 7. Reliability of Systems  | 357        |
| •     |   |            |
|       | Introduction  | 357        |
| 7.2   | General View of System Reliability Computation  | 351        |
|       | 7.2.1 Classification of systems   | 359        |
|       | 7.2.2 Basic probability rules for system reliability  | 360        |
| _     | 7.2.3 Bounds for system reliability   | 363        |
| 7.3   | Reliability of Simple Systems   | 37         |
|       | 7.3.1 Series systems  | 37         |
|       | 7.3.2 Parallel systems  | 376        |
|       | 7.3.3 K-out-of-M parallel systems   | 379        |
|       | 7.3.4 Standby redundant systems   | 380        |
| 7.4   | Methods for Computing Reliability of Complex Systems  | 38         |
|       | 7.4.1 State enumeration method  | 381        |
|       | 7.4.2 Path enumeration method   | 389        |
|       | 7.4.3 Conditional probability approach 7.4.4 Fault-tree analysis  | 389<br>391 |
| 7.5   | •   |            |
| 7.5   | Summary and Conclusions   | 398        |
|       | Appendix 7A: Derivation of Bounds for Bivariate Normal Probability                                      | 399        |
|       | Problems  | 402        |
|       | References  | 404        |
| Chapt | er 8. Integration of Reliability in Optimal Hydrosystems Design   | 407        |
|       | - · · · · · · · · · · · · · · · · · · ·   |            |
| 8.1   | Introduction  | 407        |
|       | 8.1.1 General framework of optimization models 8.1.2 Single-objective versus multiobjective programming | 400        |
|       | 8.1.3 Optimization techniques   | 409        |
|       |   | 411        |
| 5.2   | Optimization of System Reliability  | 423        |
|       | 8.2.1 Reliability design with redundancy  | 427        |
|       | 8.2.2 Determination of optimal maintenance schedule   | 429        |

|     |   | Contents | ix  |
|-----|---|----------|-----|
| 8.3 | Optimal Risk-Based Design of Hydrosystem Infrastructures            |          | 427 |
|     | 8.3.1 Basic concept   |          | 428 |
|     | 8.3.2 Historical development of hydraulic design methods            |          | 429 |
|     | 8.3.3 Tangible costs in risk-based design                           |          | 431 |
|     | 8.3.4 Evaluations of annual expected flood damage cost              |          | 433 |
|     | 8.3.5 Risk-based design without flood damage information            |          | 436 |
|     | 8.3.6 Risk-based design considering intangible factors              |          | 438 |
| 8.4 | Applications of Risk-Based Hydrosystem Design                       |          | 439 |
|     | 8.4.1 Optimal risk-based pipe culvert for roadway drainage          |          | 440 |
|     | 8.4.2 Risk-based analysis for flood-damage-reduction projects       |          | 445 |
| 8.5 | Optimization of Hydrosystems by Chance-Constrained Methods          |          | 449 |
| 8.6 | <b>Chance-Constrained Method to ASSESS Water-Quality Management</b> |          | 454 |
|     | 8.6.1 Optimal stochastic waste-load allocation                      |          | 455 |
|     | 8.6.2 Multiobjective stochastic waste-load allocation               |          | 465 |
|     | Appendix 8A: Derivation of Water-Quality Constraints                |          | 470 |
|     | Problems  |          | 472 |
|     | References  |          | 477 |