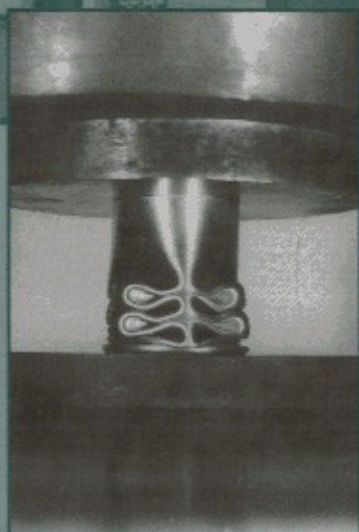


BUCKLING EXPERIMENTS

Experimental Methods in Buckling
of Thin-Walled Structures

Volume 2

Shells,
Built-up
Structures,
Composites,
and
Additional
Topics



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