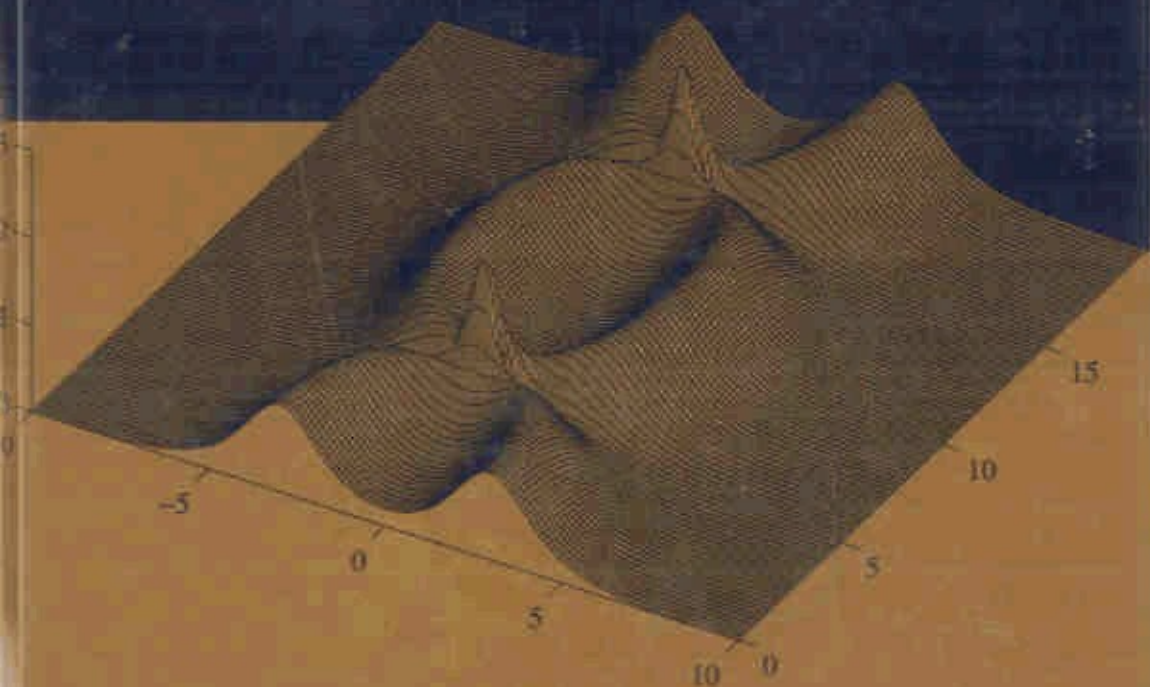


Foundations for

GUIDED-WAVE OPTICS



Chin-Lin Chen

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