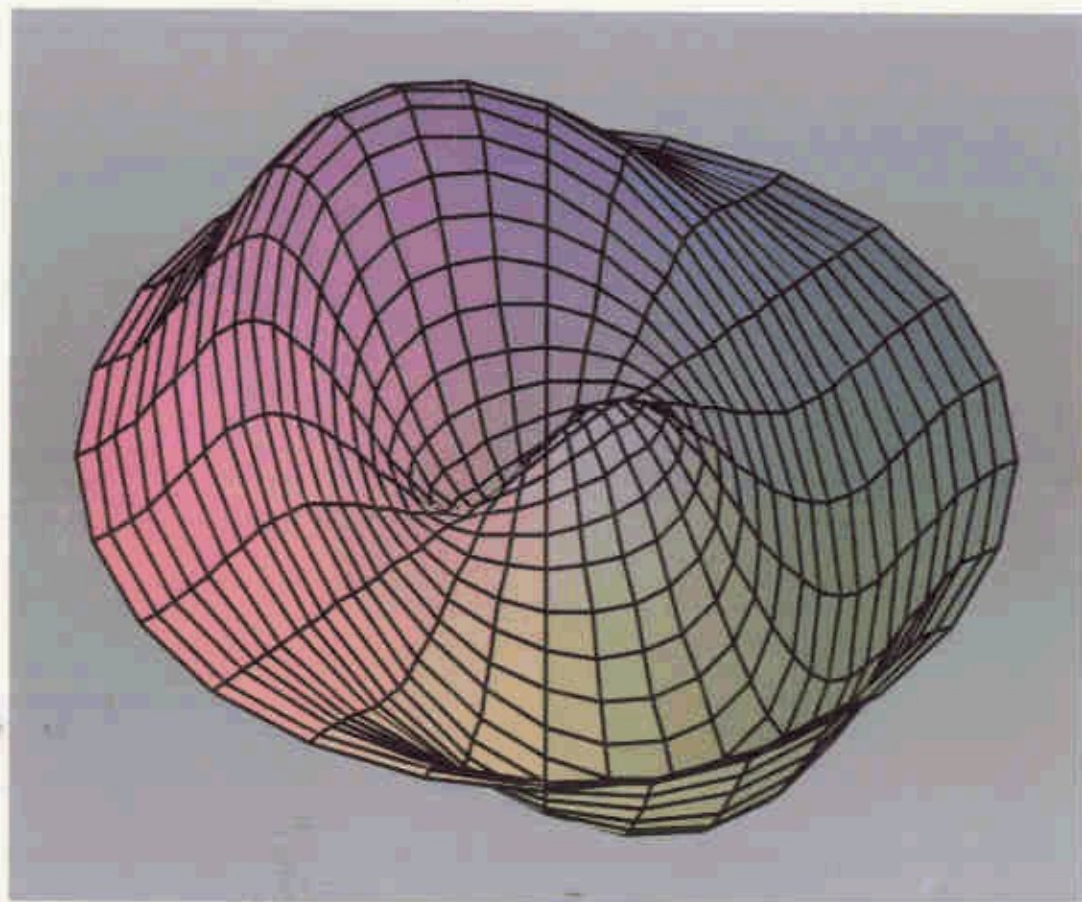


Frank Y. Wang

Physics with MAPLE

The Computer Algebra Resource for
Mathematical Methods in Physics



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