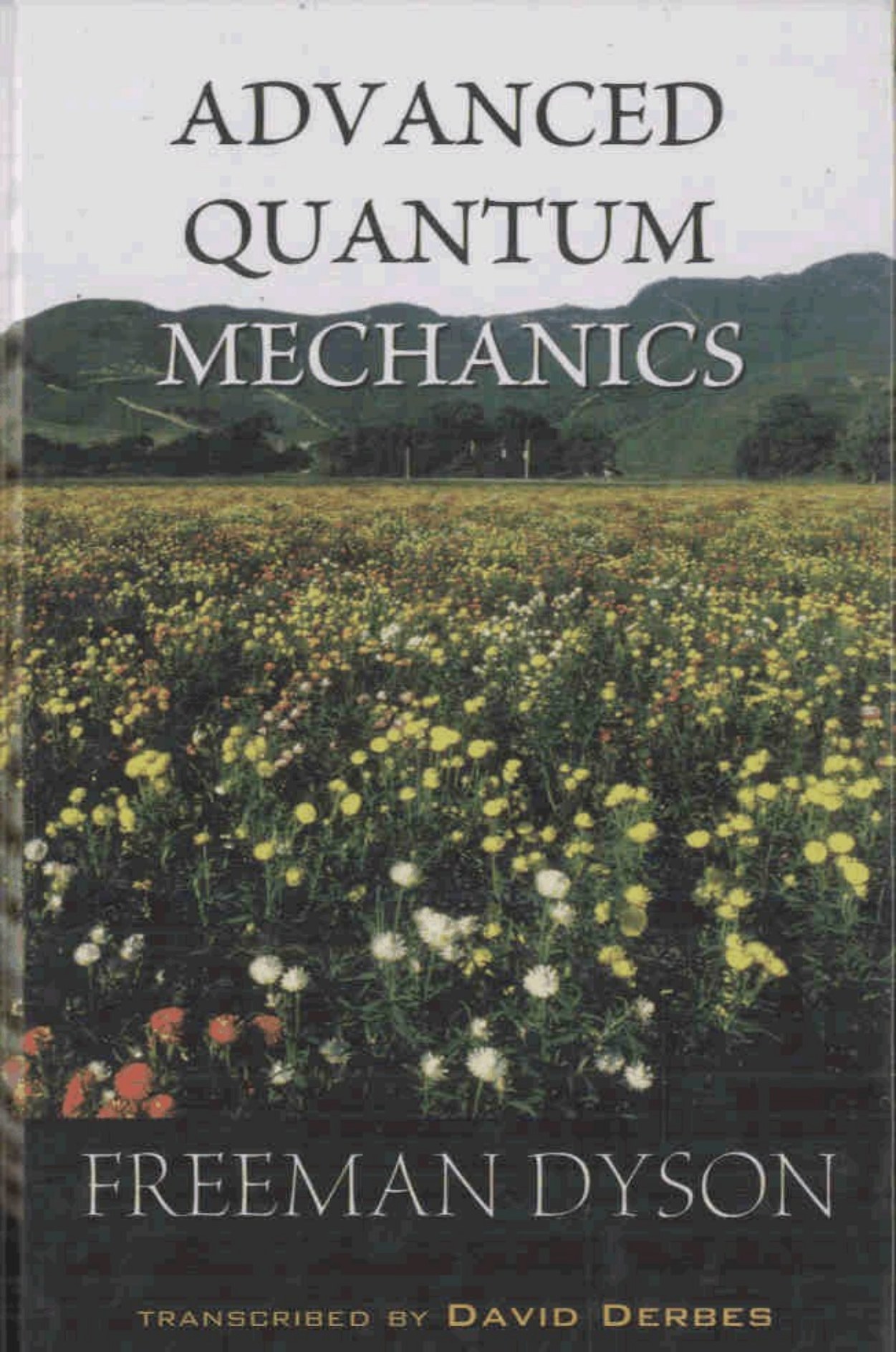




ADVANCED QUANTUM MECHANICS

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TRANSCRIBED BY **DAVID DERBES**

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