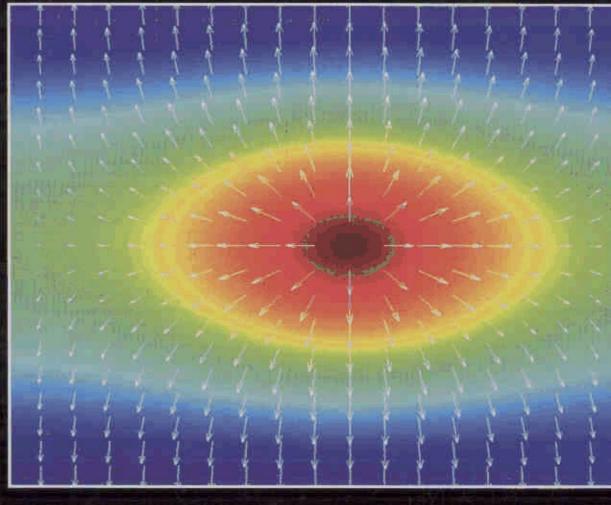
Numerical Methods for Chemical Engineering

Applications in MATLAB®



Kenneth J. Beers

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Contents

	Preface	page ix
1	Linear algebra	1
	Linear systems of algebraic equations	1
	Review of scalar, vector, and matrix operations	3
	Elimination methods for solving linear systems	10
	Existence and uniqueness of solutions	23
	The determinant	32
	Matrix inversion	36
	Matrix factorization	38
	Matrix norm and rank	44
	Submatrices and matrix partitions	44
	Example. Modeling a separation system	45
	Sparse and banded matrices	46
	MATLAB summary	56
	Problems	57
2	Nonlinear algebraic systems	61
	Existence and uniqueness of solutions to a nonlinear algebraic equation	61
	Iterative methods and the use of Taylor series	62
	Newton's method for a single equation	63
	The secant method	69
	Bracketing and bisection methods	70
	Finding complex solutions	70
	Systems of multiple nonlinear algebraic equations	71
	Newton's method for multiple nonlinear equations	72
	Estimating the Jacobian and quasi-Newton methods	77
	Robust reduced-step Newton method	79
	The trust-region Newton method	81
	Solving nonlinear algebraic systems in MATLAB	83
	Example. 1-D laminar flow of a shear-thinning polymer melt	85
	Homotopy	88
	Example. Steady-state modeling of a condensation	
	polymerization reactor	89

vi	Contents
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	Bifurcation analysis	94
	MATLAB summary	98
	Problems	99
3	Matrix eigenvalue analysis	104
	Orthogonal matrices	104
	A specific example of an orthogonal matrix	105
	Eigenvalues and eigenvectors defined	106
	Eigenvalues/eigenvectors of a 2×2 real matrix	107
	Multiplicity and formulas for the trace and determinant	109
	Eigenvalues and the existence/uniqueness properties of linear	
	systems	110
	Estimating eigenvalues; Gershgorin's theorem	111
	Applying Gershgorin's theorem to study the convergence of iterative	
	linear solvers	114
	Eigenvector matrix decomposition and basis sets	117
	Numerical calculation of eigenvalues and eigenvectors in MATLAB	123
	Computing extremal eigenvalues	126
	The QR method for computing all eigenvalues	129
	Normal mode analysis	134
	Relaxing the assumption of equal masses	136
	Eigenvalue problems in quantum mechanics	137
	Single value decomposition SVD	141
	Computing the roots of a polynomial	148
	MATLAB summary	149
	Problems	149
4	Initial value problems	154
	Initial value problems of ordinary differential equations	
	(ODE-IVPs)	155
	Polynomial interpolation	156
	Newton-Cotes integration	162
	Gaussian quadrature	163
	Multidimensional integrals	167
	Linear ODE systems and dynamic stability	169
	Overview of ODE-IVP solvers in MATLAB	176
	Accuracy and stability of single-step methods	185
	Stiff stability of BDF methods	192
	Symplectic methods for classical mechanics	194
	Differential-algebraic equation (DAE) systems	195
	Parametric continuation	203
	MATLAB summary	207
	Problems	208

Contents	vii
Comemo	

5	Numerical optimization	212
	Local methods for unconstrained optimization problems	212
	The simplex method	213
	Gradient methods	213
	Newton line search methods	223
	Trust-region Newton method	225
	Newton methods for large problems	227
	Unconstrained minimizer fminunc in MATLAB	228
	Example. Fitting a kinetic rate law to time-dependent data	230
	Lagrangian methods for constrained optimization	231
	Constrained minimizer fmincon in MATLAB	242
	Optimal control	246
	MATLAB summary	252
	Problems	252
6	Boundary value problems	258
	BVPs from conservation principles	258
	Real-space vs. function-space BVP methods	260
	The finite difference method applied to a 2-D BVP	260
	Extending the finite difference method	264
	Chemical reaction and diffusion in a spherical catalyst pellet	265
	Finite differences for a convection/diffusion equation	270
	Modeling a tubular chemical reactor with dispersion; treating	
	multiple fields	279
	Numerical issues for discretized PDEs with more than two	
	spatial dimensions	282
	The MATLAB 1-D parabolic and elliptic solver pdepe	294
	Finite differences in complex geometries	294
	The finite volume method	297
	The finite element method (FEM)	299
	FEM in MATLAB	309
	Further study in the numerical solution of BVPs	311
	MATLAB summary	311
	Problems	312
7	Probability theory and stochastic simulation	317
	The theory of probability	317
	Important probability distributions	325
	Random vectors and multivariate distributions	336
	Brownian dynamics and stochastic differential equations	
	(SDEs)	338
	Markov chains and processes; Monte Carlo methods	353
	Genetic programming	362

viii Conter

	MATLAB summary	364
	Problems	365
0	Boundary destates and an extension	2.55
8	Bayesian statistics and parameter estimation	372
	General problem formulation	372
	Example. Fitting kinetic parameters of a chemical reaction	373
	Single-response linear regression	377
	Linear least-squares regression	378
	The Bayesian view of statistical inference	381
	The least-squares method reconsidered	388
	Selecting a prior for single-response data	389
	Confidence intervals from the approximate posterior density	395
	MCMC techniques in Bayesian analysis	403
	MCMC computation of posterior predictions	404
	Applying eigenvalue analysis to experimental design	412
	Bayesian multi response regression	414
	Analysis of composite data sets	421
	Bayesian testing and model criticism	426
	Further reading	431
	MATLAB summary	431
	Problems	432
9	Fourier analysis	43€
	Fourier series and transforms in one dimension	43€
	1-D Fourier transforms in MATLAB	445
	Convolution and correlation	447
	Fourier transforms in multiple dimensions	450
	Scattering theory	452
	MATLAB summary	459
	Problems	459
	References	461
	Index	464

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