

The book cover features a dark red background with a subtle grid of thin lines. Three overlapping horizontal rectangles are positioned at the top: a light orange one on top, a light green one in the middle, and a light blue one at the bottom. The title is printed in white serif font across these rectangles. Below the title, the text 'Fourth Edition' is centered. The lower half of the cover is decorated with three sets of horizontal wave patterns. The left set consists of five yellow-green waves, the middle set consists of five blue waves, and the right set consists of five yellow waves. Each set of waves is centered horizontally and has a horizontal line passing through its peak.

Applied Statistics
and Probability
for Engineers

Fourth Edition

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