ELSEVIER AEROSPACE ENGINEERING SERIES

MICHAEL V. COOK

SECOND EDITION

Flight Dynamics PRINCIPLES

A Linear Systems Approach to Aircraft Stability and Control

B H

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