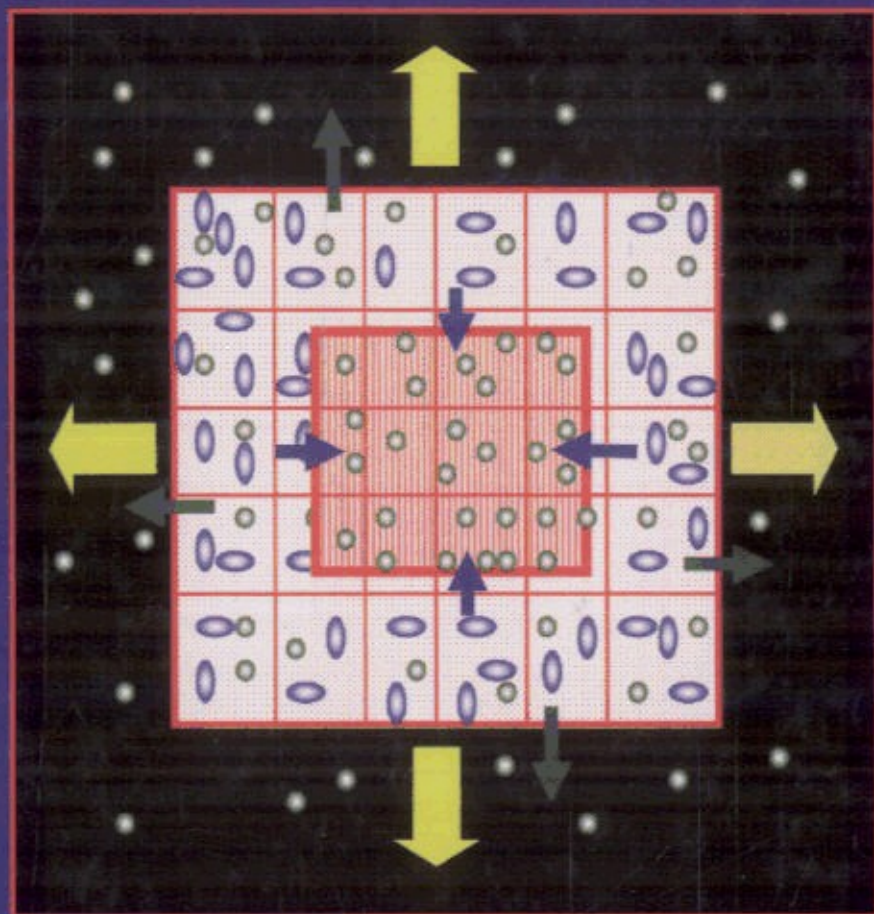


# Understanding Drug Release and Absorption Mechanisms

A PHYSICAL and  
MATHEMATICAL APPROACH



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# Table of Contents

## Chapter 1

Mathematical Modeling.....	1
1.1 Introduction.....	1
1.2 Model Building.....	3
1.2.1 Model Building: An Example .....	8
1.3 Model Fitting .....	11
1.3.1 Chi-Square Fitting: Straight Line .....	19
1.3.2 Chi-Square Fitting: General Case.....	21
1.3.3 Robust Fitting .....	22
1.4 Models Comparison.....	25
1.5 Conclusions.....	26
References.....	26

## Chapter 2

Part 1 Gastrointestinal Tract.....	29
2.1 Macro- and Microscopic Anatomy of the Gastrointestinal Tract .....	29
2.1.1 The Stomach .....	29
2.1.2 The Small Intestine .....	30
2.1.3 The Colon .....	32
2.1.4 Absorptive Cells .....	32
2.1.5 Tight Junctions.....	33
2.1.6 Cellular Membrane .....	34
2.2 Intestinal Absorption .....	35
2.2.1 Positive and Negative Forces .....	35
2.2.2 Drug Absorption Pathways.....	36
2.2.3 Absorption in GI Diseases.....	38
2.2.4 Models of Intestinal Absorption.....	40
2.3 Human and Animal GI Tract: A Comparison .....	42
2.3.1 Anatomy.....	42
2.3.1.1 The Stomach .....	42
2.3.1.2 The Small Intestine.....	43
2.3.1.3 The Colon .....	43
2.3.2 Physiology.....	45
2.3.2.1 pH and Bile Fluid .....	45
2.3.2.2 Microflora and Mucin .....	49

2.3.2.3	Other Physiological Aspects .....	50
2.3.3	GI Tract Biochemistry .....	51
Part 2	Skin.....	53
2.4	Anatomy.....	53
2.4.1	Epidermis .....	53
2.4.1.1	Stratum Corneum Structure.....	56
2.4.2	Dermis.....	56
2.4.3	Hypodermis.....	58
2.5	Skin Delivery Strategies.....	58
2.5.1	Electrically Based Enhancement.....	59
2.5.2	Vesicular Carriers .....	62
2.5.3	Chemical Enhancement .....	63
2.5.4	Microinvasive Delivery .....	64
2.5.5	Velocity-Based Technique.....	64
2.6	Animal Model of Skin Delivery.....	65
2.6.1	Pig .....	65
2.6.2	Mouse.....	66
References	.....	68

### Chapter 3

Rheology .....	89	
3.1	Introduction.....	89
3.2	Viscosity and Newtonian Fluids .....	91
3.3	Shear-Dependent Viscosity and Non-Newtonian Fluids .....	95
3.4	Shear Flows .....	99
3.5	Not Only Viscosity: Normal Stress Differences and Other Material Functions.....	102
3.5.1	Tensional State.....	102
3.5.2	Deformation State.....	105
3.5.3	Normal Stress Differences.....	107
3.6	Extensional Flows and Complex Flows.....	108
3.7	Time-Dependence: Thixotropy and Viscoelasticity .....	112
3.8	Linear Viscoelasticity .....	116
3.8.1	Oscillatory Shear Test and Linear Viscoelastic Quantities ...	116
3.8.2	Linear Viscoelastic Models .....	118
3.9	Rheological Properties and Structural Features .....	123
3.9.1	Simple Fluids and Homogeneous Mixtures .....	124
3.9.1.1	Salt Solutions.....	125
3.9.2	Surfactant Solutions (From Dilute to Micellar and Crystalline Systems) .....	126
3.9.3	Polymeric Systems.....	129

3.9.3.1	Flexible Chains and Ordinary Polymer Solutions.....	129
3.9.3.2	Rigid Chains and Crystalline Polymer Solutions ...	135
3.9.3.3	Time Temperature Superposition Principle .....	139
3.9.3.4	Associative Polymer Solutions and Gels .....	140
3.9.3.5	Weak and Strong Physical Gels .....	143
3.9.4	Disperse Systems .....	145
3.9.4.1	Colloidal Interactions and Dispersion State.....	146
3.9.4.2	Suspensions of Noninteracting Particles (Hard Sphere Model).....	149
3.9.4.3	Effects of Particle Size Distribution and Shape .....	152
3.9.4.4	Suspensions of Stabilized Particles .....	154
3.9.4.5	Suspensions of Attractive Particles .....	155
3.9.4.6	Emulsions.....	159
3.9.4.7	Microemulsions .....	163
3.9.4.8	Dispersions in Polymeric Matrices .....	163
3.10	Conclusive Considerations on Rheology Applications to Drug Delivery Systems .....	164
	References.....	168

## Chapter 4

	Mass Transport .....	177
4.1	Introduction.....	177
4.2	Thermodynamic Concepts .....	179
4.2.1	Thermodynamic Equilibrium.....	180
4.2.2	Gibbs–Duhem Equation.....	183
4.2.3	Thermodynamic Potentials .....	184
4.3	Kinetics .....	185
4.3.1	Mass Conservation Law .....	187
4.3.2	Momentum Conservation Law .....	192
4.3.3	Energy Conservation Law .....	198
4.3.4	Final Considerations .....	201
4.4	Fick’s Equation.....	202
4.4.1	Diffusion Coefficient .....	202
4.4.1.1	Diffusion in Solid or Solid-Like Medium.....	204
4.4.2	Fickian Kinetics .....	215
4.5	Effect of Initial and Boundary Conditions.....	218
4.5.1	Finite Release Environment Volume and Partition Coefficient.....	219
4.5.2	Initial Drug Distribution .....	221
4.5.3	Stagnant Layer .....	230
4.5.4	Holed Surfaces.....	231
4.5.4.1	Buchtel Model .....	236

4.6	Conclusions.....	244
	References.....	246

## Chapter 5

	Drug Dissolution and Partitioning .....	249
5.1	Introduction.....	249
5.2	Dissolution.....	251
5.2.1	Surface Properties .....	253
5.2.1.1	Young's Equation .....	255
5.2.1.2	Surface Tension Determination.....	259
5.2.1.3	Wettability Effect on Drug Dissolution .....	265
5.2.2	Hydrodynamics .....	271
5.2.2.1	Rotating Disk Apparatus .....	272
5.2.2.2	Fixed Disk Apparatus .....	280
5.2.2.3	USP Apparatus.....	282
5.2.2.4	Channel Flow Method .....	285
5.2.3	Drug Solubility and Stability.....	288
5.2.3.1	Dissolution and Phase Changes.....	289
5.2.3.2	Dissolution of Polyphase Mixtures .....	291
5.2.3.3	Dissolution of Polyphase Mixtures: A Particular Case .....	297
5.2.3.4	Dissolution and Drug Degradation.....	301
5.2.4	Dissolution of Particulate Systems.....	302
5.3	Partitioning.....	306
5.3.1	Three Phases Partitioning .....	313
5.3.2	Partitioning and Permeation .....	318
5.3.3	Log( <i>P</i> ) Calculation .....	320
5.4	Dissolution and Partitioning.....	321
5.5	Conclusions.....	324
	References.....	327

## Chapter 6

	Dissolution of Crystallites: Effects of Size on Solubility .....	333
6.1	Introduction.....	333
6.2	Thermodynamic Concepts.....	334
6.2.1	Ideal Solutions .....	335
6.2.2	Melting Temperature Dependence on Crystal Dimension .....	340
6.2.3	Solubility Dependence on Crystal Dimension .....	350
6.2.3.1	Liquid–Vapor System.....	350
6.2.3.2	Solid–Liquid System .....	352
6.3	Experimental Methods and Limitations .....	354
6.4	Conclusions.....	365
	References.....	366

## Chapter 7

Drug Release from Matrix Systems .....	371
7.1 Introduction.....	371
7.2 Matrices .....	372
7.2.1 Matrix Topology.....	373
7.2.2 Release Mechanisms.....	381
7.3 Mathematical Modeling.....	387
7.3.1 Diffusion-Controlled Systems .....	394
7.3.2 Diffusion and Matrix/Drug Interactions Controlled Systems.....	401
7.3.3 Diffusion and Chemical Reaction Controlled Systems .....	411
7.3.4 Diffusion- and Dissolution-Controlled Systems .....	414
7.3.5 Diffusion-, Dissolution-, and Swelling- Controlled Systems.....	429
7.3.5.1 Matrix Swelling Equilibrium.....	429
7.3.5.2 Matrix Swelling Kinetics.....	439
7.3.5.3 Drug Dissolution and Diffusion .....	449
7.3.6 Erosion-Controlled Systems .....	452
7.3.7 Polydisperse Systems.....	460
7.3.8 Diffusion in Fractal Matrices .....	474
7.4 Conclusions.....	478
References.....	479

## Chapter 8

Drug Release from Microemulsions .....	493
8.1 Introduction.....	493
8.2 Microemulsions: Structure .....	495
8.3 Microemulsions: Thermodynamics .....	498
8.3.1 Discrete Microemulsions' Droplet Size Distribution.....	499
8.3.2 Liquid-Liquid Interfacial Composition.....	500
8.4 Microemulsions: Experimental Characterization.....	509
8.4.1 Scattering Techniques.....	509
8.4.2 Nuclear Magnetic Resonance Techniques .....	510
8.4.3 Electronic Microscopy.....	510
8.4.4 Conductivity and Dielectric Spectroscopy.....	511
8.4.5 Rheology .....	511
8.5 Microemulsions and Drug Release .....	512
8.5.1 Microemulsion Administration Routes .....	513
8.5.2 Modeling of Drug Release from Microemulsions .....	515
8.5.2.1 Simple Case .....	519
8.5.2.2 More Complex Situation .....	525
8.6 Conclusions.....	534
References.....	535

## **Chapter 9**

Drug Permeation through Membranes .....	539
9.1 Introduction.....	539
9.2 Synthetic Membranes .....	540
9.2.1 Synthetic Membranes Permeability Determination .....	541
9.2.2 Microencapsulated Systems.....	550
9.2.2.1 Physical Frame .....	551
9.2.2.2 Modeling.....	553
9.3 Biological Membranes.....	565
9.3.1 Intestinal Mucosa.....	565
9.3.1.1 <i>In Silico</i> Methods.....	565
9.3.1.2 Physicochemical Methods.....	567
9.3.1.3 <i>In Vitro</i> Methods.....	569
9.3.1.4 <i>In Situ</i> Methods.....	571
9.3.1.5 <i>In Vivo</i> Methods .....	571
9.3.1.6 Modeling: Everted Gut.....	572
9.3.1.7 Modeling: Single Pass and Recirculating Perfusion .....	575
9.3.2 Skin .....	583
9.3.2.1 Mechanistic Models.....	586
9.3.2.2 Empirical Models .....	596
9.4 Conclusions.....	598
References.....	598
<b>Index.....</b>	<b>607</b>