

UNDERSTANDING
COMPLEX SYSTEMS

Springer:
COMPLEXITY

Boris S. Kerner

The Physics of Traffic

Empirical Freeway Pattern Features,
Engineering Applications,
and Theory



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