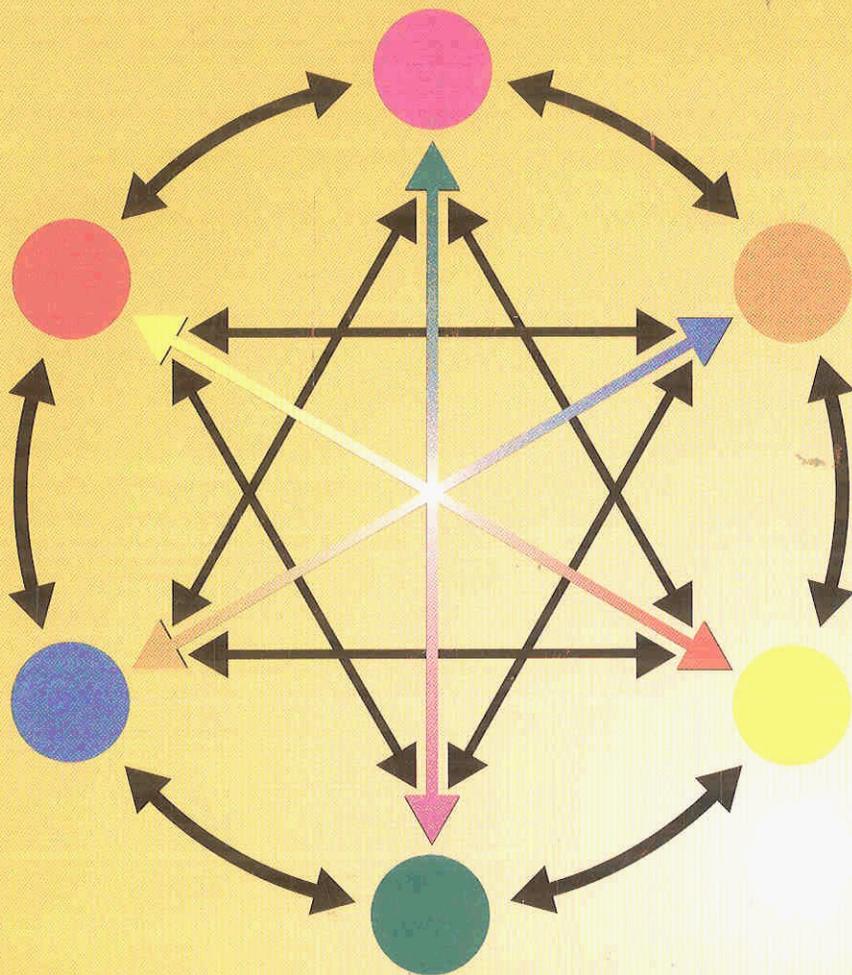


Theory and Applications of the Analytic Network Process

Decision Making with Benefits, Opportunities,
Costs, and Risks

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