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Piezoelectric Multilayer Beam Bending Actuators

Static and Dynamic
Behavior and Aspects
of Sensor Integration



Springer

Contents

List of Symbols	XV
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Part I Focus of the Book

1 Introduction	3
1.1 Application Areas of Piezoelectric Actuators	3
1.2 Motivation and Aim of the Book	4
1.3 State of the Scientific Research	6
1.4 Textual Focus of the Book	11

Part II Theoretical Aspects and Closed Form Analysis

2 Piezoelectric Materials	17
2.1 Discovery of Piezoelectricity	17
2.2 Direct and Inverse Piezoelectric Effect	18
2.3 Piezoelectric Ceramics	19
2.4 Perovskit Structure of PZT	20
2.5 Domain and Reversion Processes of PZT	21
2.6 Electromechanical Behavior	24
2.7 Piezoelectric Beam Bending Actuators	26
3 Linear Theory of Piezoelectric Materials	31
3.1 Energy Density of the Elastic Deformation	31
3.2 Energy Density of the Electrostatic Field	35
3.3 Thermodynamics of Deformation	36
3.3.1 Internal Energy of Elastic Piezoelectric Materials	38
3.3.2 Linear Constitutive Equations and Electrical Enthalpy ..	39
3.3.3 Condensed Notation of Elastic and Piezoelectric Tensors	43

4	Theory of the Static Behavior of Piezoelectric Beam	
	Bending Actuators	47
4.1	Sectional Quantities of a Bending Beam	47
4.2	Bernoulli Hypothesis of Beam Bending Theory	49
4.3	Neutral Axis Position of a Multilayered Beam Bender	51
4.4	Forces and Moments within a Multilayer System	54
4.5	Total Stored Energy within a Multilayer System	55
	4.5.1 Total Energy in a Single Layer	56
	4.5.2 Energy in an n -layered System	57
4.6	Canonical Conjugates and Coupling Matrix	58
4.7	Principle of Virtual Work	60
4.8	Theorem of Minimum Total Potential Energy	61
4.9	Derivation of the Coupling Matrix	62
	4.9.1 Multilayer Beam Bender Subjected to an External Static Moment	63
	4.9.2 Multilayer Beam Bender Subjected to an External Static Force	65
	4.9.3 Multilayer Beam Bender Subjected to a Uniform Pressure Load	67
	4.9.4 Electrical Charge Generated by the Extensive Parameters	69
4.10	The Constituent Equations	75
5	Piezoelectric Beam Bending Actuators and Hamilton's Principle	77
5.1	Constraints and Generalized Coordinates	77
5.2	D'Alembert's Principle	78
5.3	Lagrange's Equations	80
5.4	Euler-Lagrange Differential Equation	83
5.5	Hamilton's Principle	87
5.6	Consideration of Non-Conservative Forces	88
5.7	Lagrange Function of Piezoelectric Beam Bending Actuators ..	91
5.8	Mechanical Work Done by Extensive Quantities and Frictional Force	95
5.9	Variation of the Lagrange Function	98
5.10	Variation of the Mechanical Work	99
5.11	Differential Equations of a Piezoelectric Multilayer Beam Bender	100
6	Theory of the Dynamic Behavior of Piezoelectric Beam	
	Bending Actuators	103
6.1	Eigenmodes of a Clamped-Free Beam Bender	103
6.2	Orthogonality of Eigenfunctions	107
6.3	Description of Flexural Vibrations with Respect to Time	109
6.4	The Free Damped Flexural Vibration	110

6.5	Excitation by a Harmonic Force	112
6.6	Excitation by a Harmonic Moment	114
6.7	Excitation by a Harmonic Uniform Pressure Load	116
6.8	Excitation by a Harmonic Driving Voltage	117
6.9	Electrical Charge Generated by Harmonic Extensive Parameters	118
6.10	Dynamic Admittance Matrix	121
7	Network Representation of Piezoelectric Multilayered Bending Actuators	123
7.1	The Ideal Rod as Transducer for Translatory and Rotatory Quantities	124
7.2	Bending of a Differential Beam Segment	126
7.3	The Differential Beam Segment and Corresponding Correlations	129
7.4	Solution Approach to the Complex Equation of Flexural Vibrations	133
7.5	General Solution of the Equation for Flexural Vibrations	135
7.5.1	Reference Values of a Multilayered Beam Bender	136
7.6	Solution of the Equation of Flexural Vibrations by Means of Reference Values	137
7.7	Admittance Matrix of a Beam Bender	137
7.7.1	Excitation by a Harmonic Force $\underline{F}_1$	138
7.7.2	Excitation by a Harmonic Force $\underline{F}_2$	139
7.7.3	Excitation by a Harmonic Moment $\underline{M}_1$	140
7.7.4	Excitation by a Harmonic Moment $\underline{M}_2$	141
7.8	Transition to the Piezoelectric Multilayer Beam Bending Actuator	142
7.9	The Clamped-Free Piezoelectric Multimorph	149
7.9.1	Circuit Representation of a Piezoelectric Multimorph with Respect to the Fundamental Mode	153
7.9.2	Canonical Circuit Representation of a Piezoelectric Multimorph	157

Part III Measurement Setup and Validation of Theoretical Aspects

8	Measurement Setup for Piezoelectric Beam Bending Actuators	163
8.1	Measurement Setup	163
8.2	Automation of Measurement Setup	167
8.2.1	Stabilization of the Beam Bending Actuator	168
8.2.2	Electrical Actuation of the Bending Actuator	169
8.2.3	Deflection Measurement by Means of Triangulation	169
8.2.4	Control of the Linear Stages	170

8.2.5	Control of the Voice-Coil-Motor	170
9	Measurements and Analytical Calculations	173
9.1	Used Multilayer Beam Bending Structure for Experimental Investigations	173
9.2	Static and Quasi-static Measurements	175
9.2.1	Hysteresis Measurement	175
9.2.2	Measurement and Analytical Calculation of Bending Curvatures Under Different Excitation Voltages	178
9.2.3	Measurement and Analytical Calculation of Force-Deflection Characteristics	180
9.2.4	Drift and Creep Measurements	182
9.3	Dynamic Measurements	184
9.3.1	Experimental Evaluation of the Coefficient of Friction ..	184
9.3.2	Measurement and Analytical Calculation of the First and Second Eigenmode	187
9.3.3	Measurement and Analytical Calculation of the Transfer Function	191

Part IV Sensor Integration for Tip Deflection Measurements

10	Piezoelectric Beam Bending Actuator with Integrated Sensor	199
10.1	Smart Pneumatic Micro Valve	200
10.2	Sensor Requirements	201
11	Tip Deflection Measurement - Capacitive Sensor Principle	203
11.1	Sensor Positioning	203
11.2	Sensor Electronics for Capacitive Strain Sensors	206
11.2.1	Electronic Circuit	206
11.2.2	Static Sensor Performance and Uncertainty of Measurement	212
11.2.3	Measurement Results	213
12	Tip Deflection Measurement - Inductive Sensor Principle	217
12.1	Measurement Setup and Basic Structure of the Inductive Proximity Sensor	217
12.2	Functioning of the Inductive Proximity Sensor	219
12.2.1	Output Signal Performance	220
12.3	Equivalent Network Representation	223
12.4	Inductance of a Circular Loop Influenced by a Conductive Layer	227
12.4.1	Solution Approach	227
12.4.2	Magnetic Field of a Circular Loop	229

12.4.3 Influence of a Conductive Layer	230
12.4.4 Relative Inductance Change of a Circular Loop in Presence of a Conductive Layer	231
12.5 Measurement Results	234
12.5.1 Relative Inductance Change of the Sensing Coil with Respect to a Conductive Copper Layer	235
12.5.2 Performance of the Inductive Proximity Sensor	240
13 Conclusion	249
13.1 Summary and Results	249
13.2 Outlook	253

Part V Appendix

A Work Done by Stresses Acting on an Infinitesimal Volume Element	257
B Derivation of the Coupling Matrix Elements	261
B.1 Multilayer Beam Bender Subjected to an External Static Moment	261
B.2 Multilayer Beam Bender Subjected to an External Static Force	264
B.3 Multilayer Beam Bender Subjected to a Uniform Pressure Load	266
B.4 Electrical Charge Generated by the Extensive Parameters ...	268
B.4.1 External Static Moment	272
B.4.2 External Static Force	273
B.4.3 External Uniform Pressure Load	275
C Mechanical Potential and Kinetic Energy	279
D Derivation of the Electrical Enthalpy	281
E Correlation Between Material Parameters	283
F Work Done by Extensive Dynamic Quantities	285
F.1 Work Done by a Force	285
F.2 Work Done by a Moment	286
F.3 Work Done by a Driving Voltage	287
G On the Variation of the Lagrange Function	289
H On the Variation of the Work Done by Extensive Quantities	295
I On the Excitation by a Periodic Force	297

J	Particular Solution of the Differential Equation for Flexural Vibrations	299
K	Transition to the Differential Equations in Complex Form	301
L	Orthogonality of Different Boundary Conditions	305
M	Logarithmic Decrement	309
N	Favored Sensor Principles and Sensor Signal Estimation	311
N.1	Resistive Distance Sensors	312
N.1.1	Metallic Strain Gages	313
N.1.2	Semiconductor Strain Gages	314
N.2	Capacitive Distance Sensors	316
N.2.1	All over Covering Electrodes (double-sided)	316
N.2.2	Interdigital Electrodes (double-sided)	318
N.3	Piezoelectric Distance Sensor	321
N.4	Inductive Distance Sensor	323
O	Methods of Measuring Small Capacitances with High Resolution	327
O.1	Direct Method	327
O.2	Self-balancing Capacitance Bridge	328
O.3	Charge Measurement	330
O.4	Measurement of the Integration Time	331
O.5	Oscillator Method	331
P	To the Output Signal of the Instrumentation Amplifier	333
Q	Alternating Magnetic Field Within a Conductive Layer	335
R	Magnetic Field Calculation of a Circular Loop	337
	References	341
	Index	353