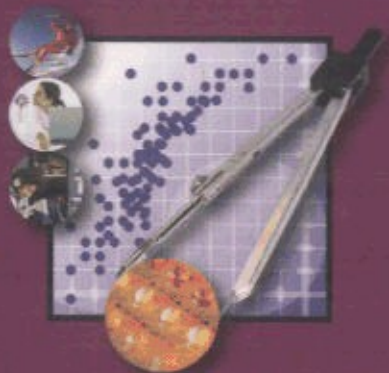


INTERNATIONAL STUDENT EDITION

DUXBURY APPLIED SERIES

EXPERIMENTAL DESIGN USING ANOVA



TABACHNICK • FIDELL

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