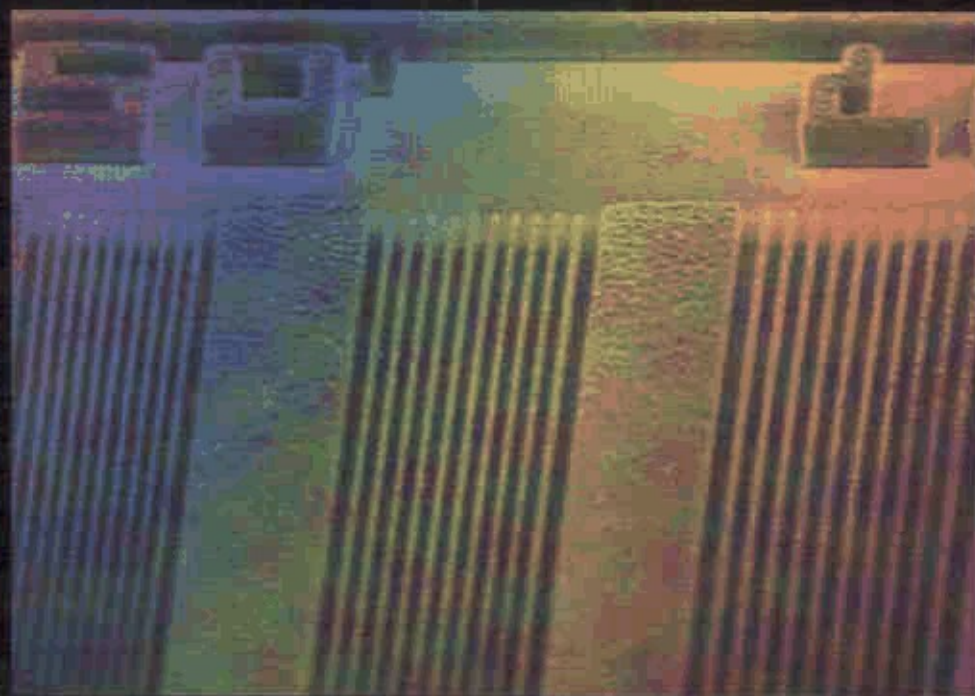


# **SOFT X-RAYS AND EXTREME ULTRAVIOLET RADIATION**

**Principles and Applications**



**DAVID ATTWOOD**

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