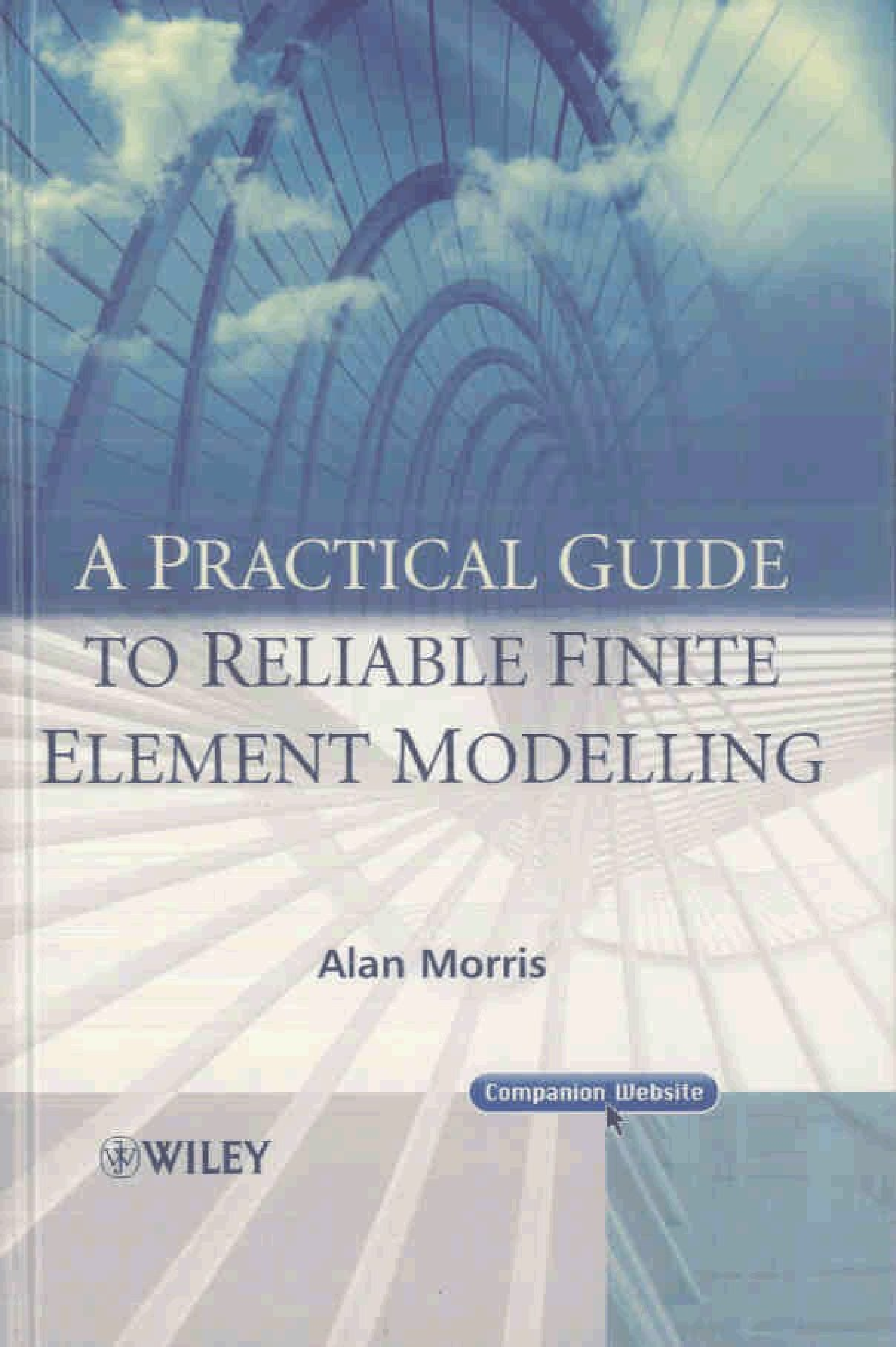

A Practical Guide to Reliable Finite Element Modelling

Alan Morris

Companion Website

WILEY

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