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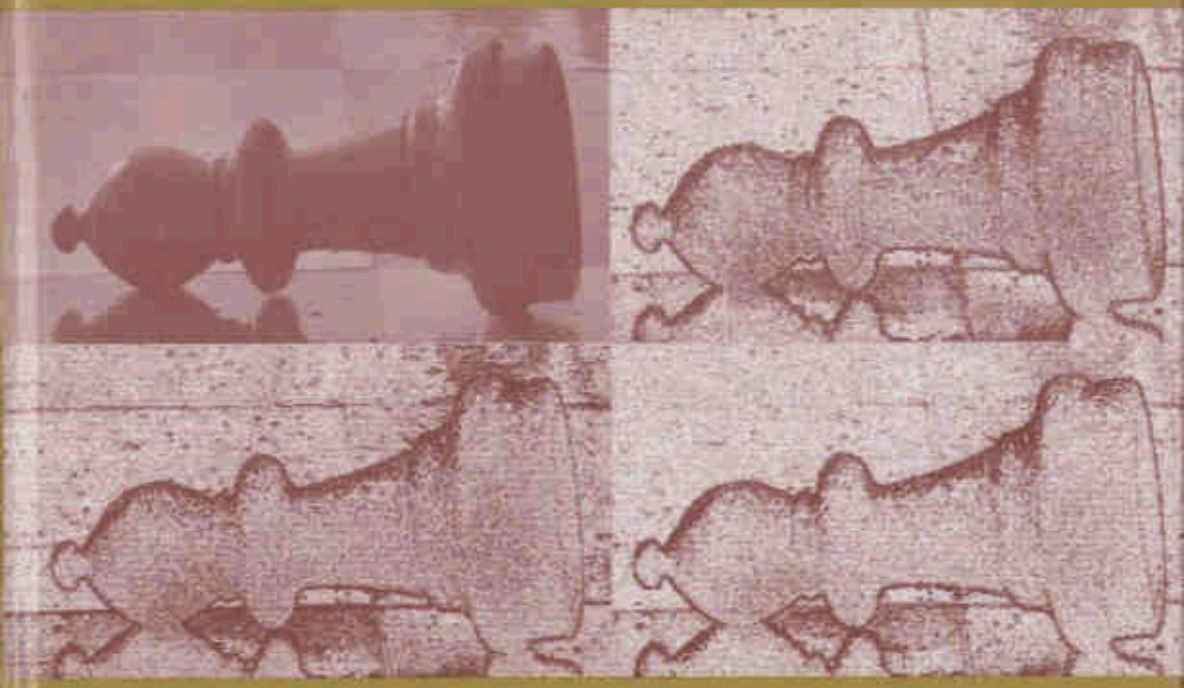

DISCRETE WAVELET TRANSFORMATIONS

An Elementary Approach with Applications

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