



A close-up photograph of a car's front left headlight and fender. The headlight is illuminated, casting a bright light. The fender is silver and shows some reflections of the surrounding environment. The background is dark and out of focus.

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Vehicle Dynamics

Theory and Application

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