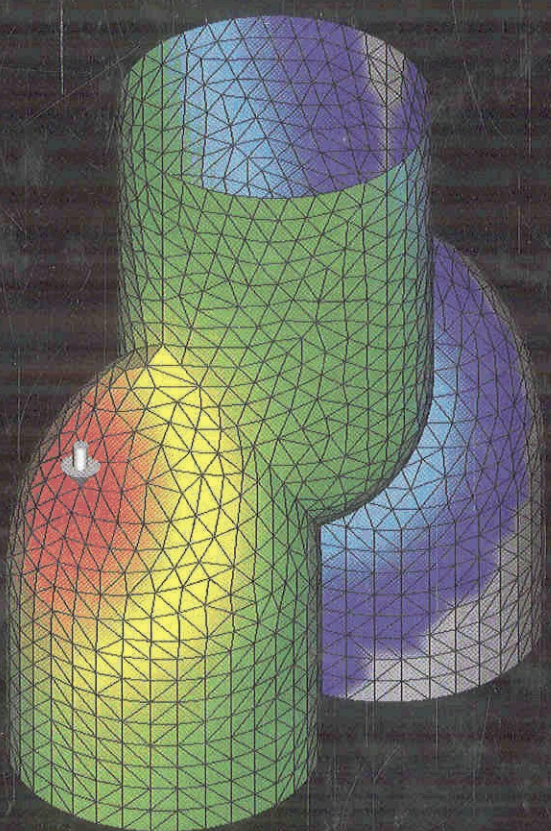
Wiley Series on Processing of Engineering Materials • Randall M. German, Series Editor

RANDALL M. GERMAN AND SEONG JIN PARK

Handbook of Mathematical Relations in Particulate Materials Processing

CERAMICS, POWDER METALS, CERMETS, CARBIDES, HARD MATERIALS, AND MINERALS



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