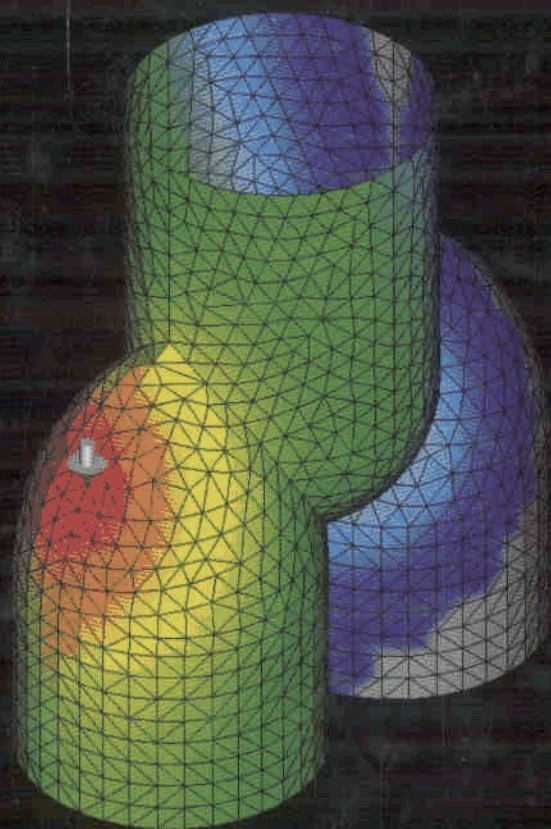


Wiley Series on Processing of Engineering Materials • Randall M. German, Series Editor

RANDALL M. GERMAN AND SEONG JIN PARK

# Handbook of Mathematical Relations in Particulate Materials Processing

CERAMICS, POWDER METALS, CERMETS,  
CARBIDES, HARD MATERIALS,  
AND MINERALS



 **WILEY**

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